

November 10-16, 2018

An-Najah N. University, Nablus, Palestine

Detection of gravitational waves

- Gravitational-wave detectors
- LIGO-Virgo detector network
- Signal extraction methods
- Detector's noise

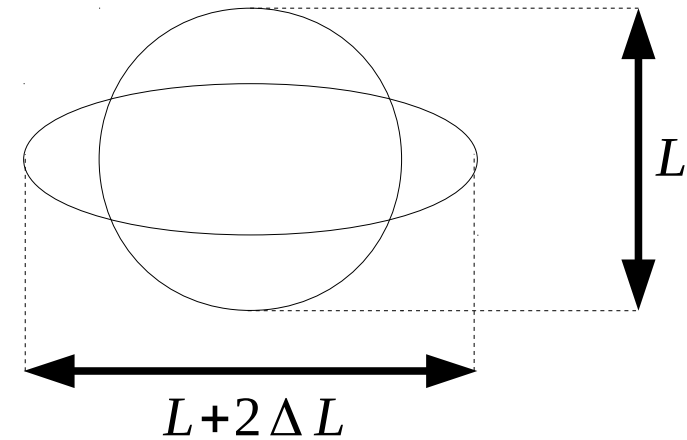
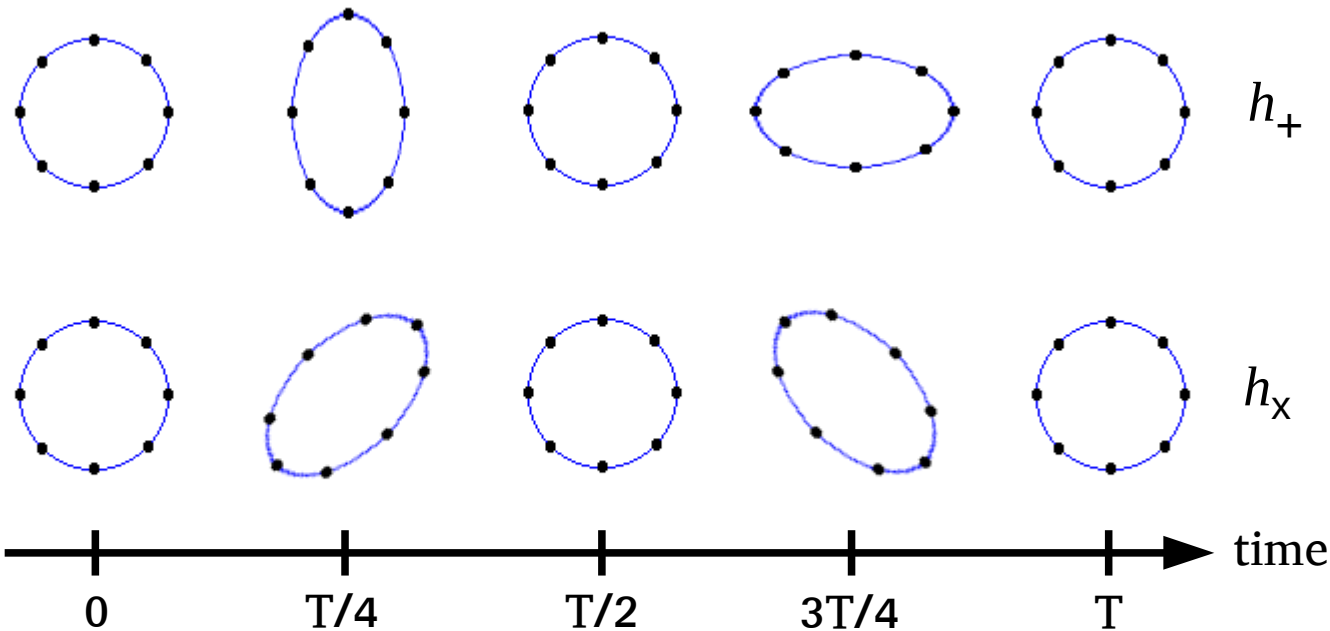


Gravitational wave detection

Add a small perturbation to the Minkowski metric: $g_{\mu\nu} = \eta_{\mu\nu} + h_{\mu\nu}$ $|h_{\mu\nu}| \ll 1$

- h obeys a plane-wave equation
- the wave propagates at the speed of light
- 2 degrees of freedom: h_+ and h_\times

→ Gravitational waves



$$h = 2 \frac{\Delta L}{L}$$

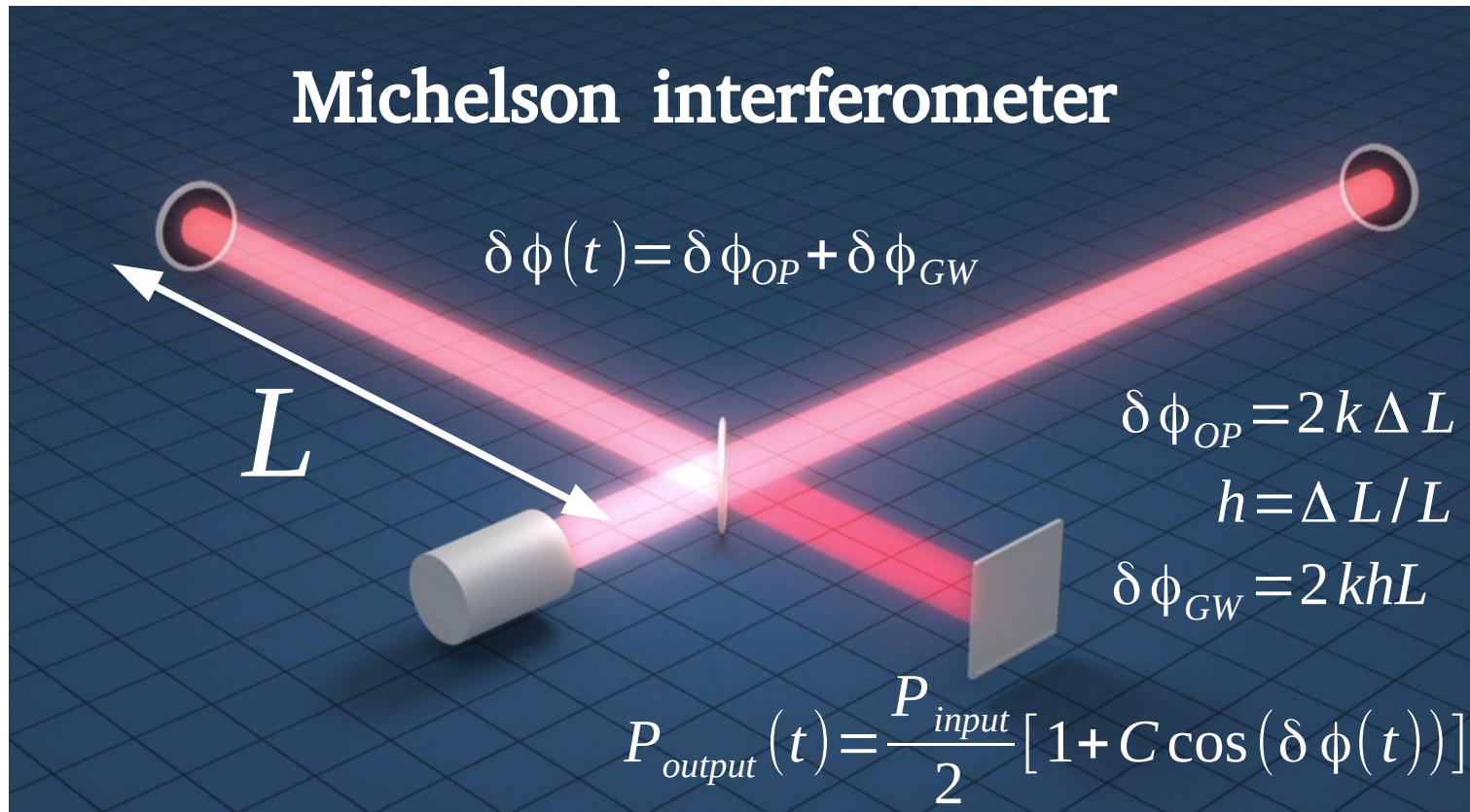
When they propagate, gravitational waves

- do not interact with matter
- are attenuated by $1/r$

→ **Gravitational waves are the perfect probe!**

→ **BUT... $h \sim 10^{-21}$**

Gravitational wave detectors



$$P_{output}(t) \simeq \frac{P_{input}}{2} [1 + C \cos(\delta \phi_{OP}) - C \sin(\delta \phi_{OP}) \times \delta \phi_{GW}(t)]$$

→ A gravitational wave is detected as a power variation

Sensitivity limited by noise

The detector's sensitivity to h is limited by noise

For example: shot noise due to uncertainty in photon counting rate

$$N_{\text{photon}} \propto P_{\text{output}} \quad \rightarrow \quad \delta N_{\text{photon}} \propto \sqrt{N_{\text{photon}}} \quad \rightarrow \quad \delta P_{\text{shotnoise}} \propto \sqrt{P_{\text{output}}}$$

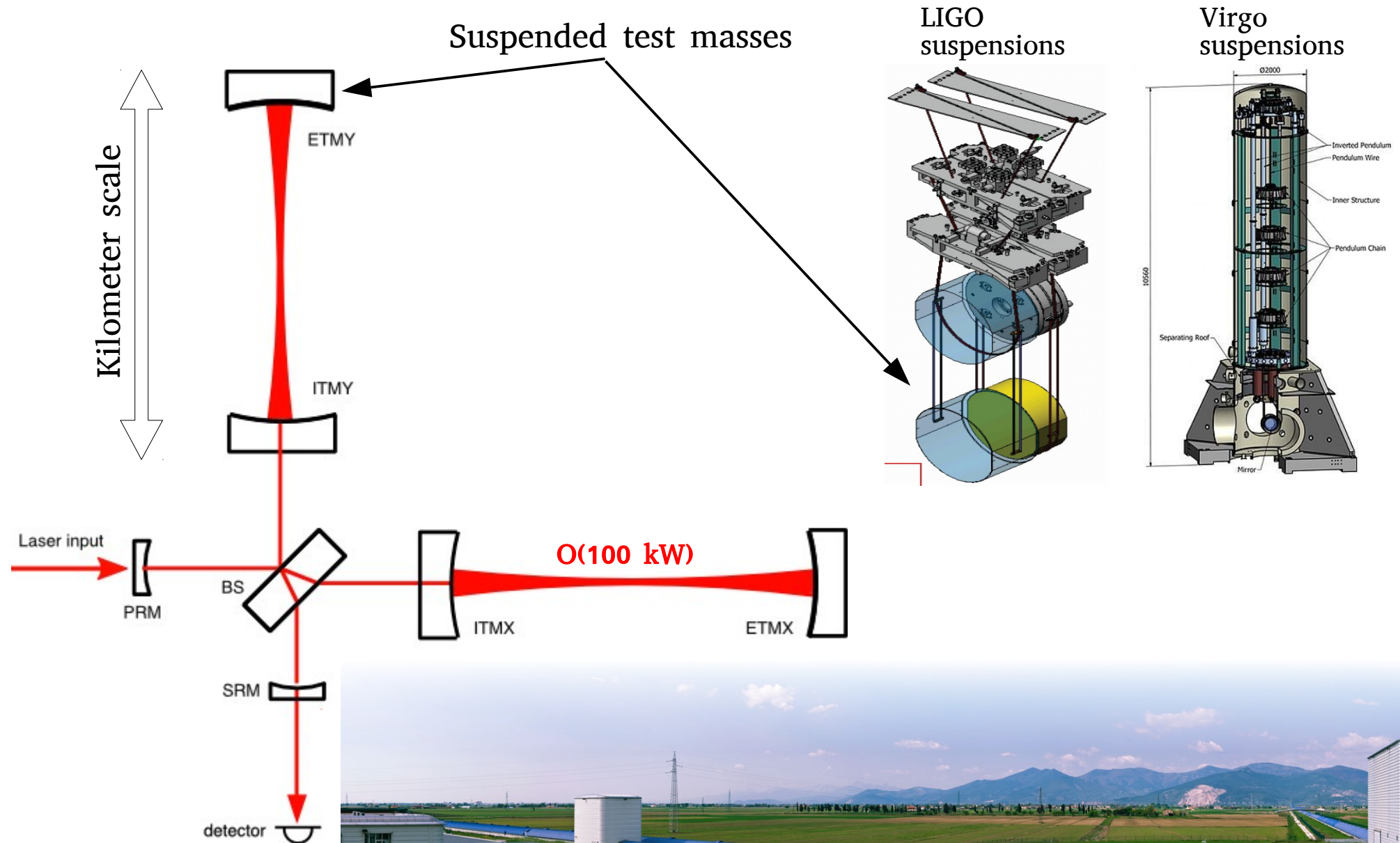
Signal-to-noise ratio

$$\frac{S}{B} = \frac{\delta P_{\text{GW}}}{\delta P_{\text{shot noise}}} \propto L \sqrt{P_{\text{input}}} h$$

$$\text{If } \frac{S}{B} = 1 \quad \rightarrow \quad h_{\text{shot noise}} \propto \frac{1}{L \sqrt{P_{\text{input}}}}$$

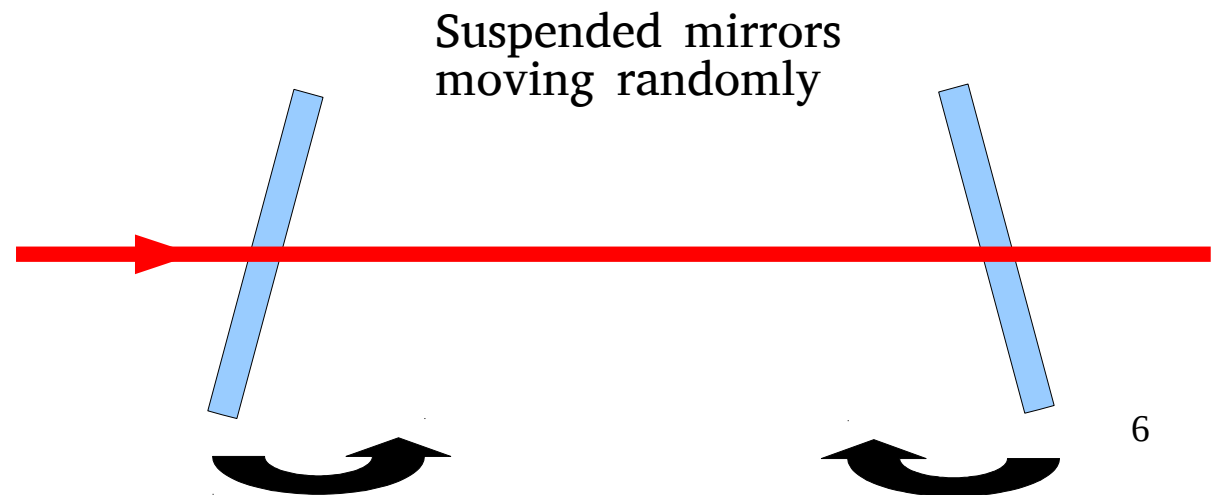
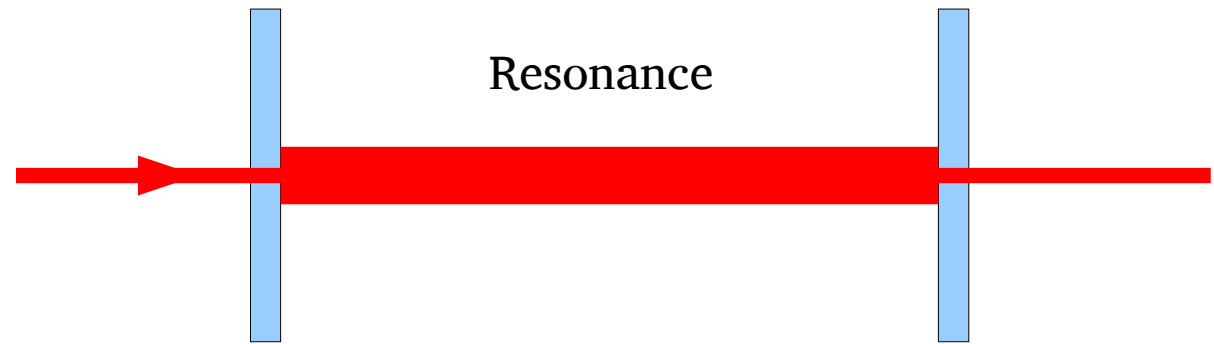
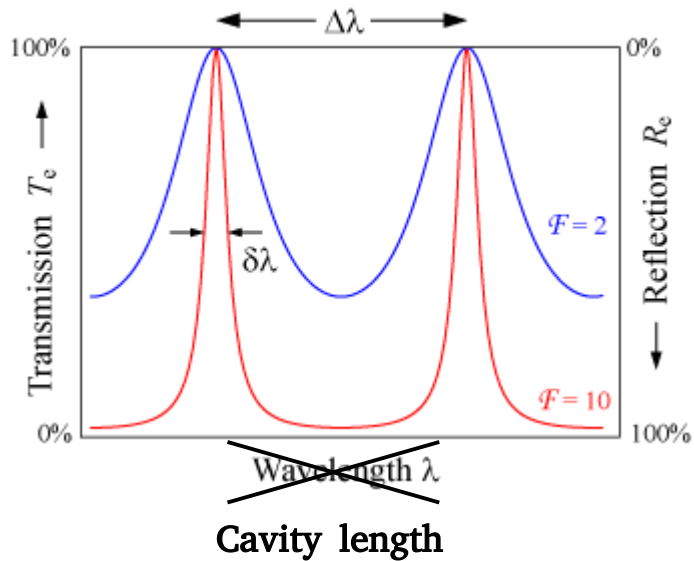
Table-top Michelson interferometer $\rightarrow 10^{-17}$

Gravitational wave detectors



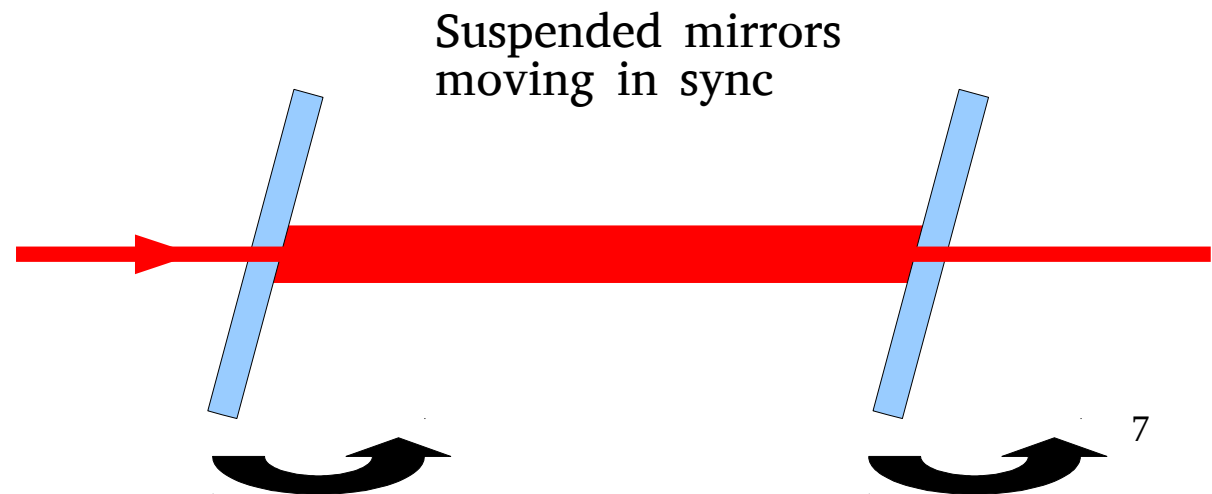
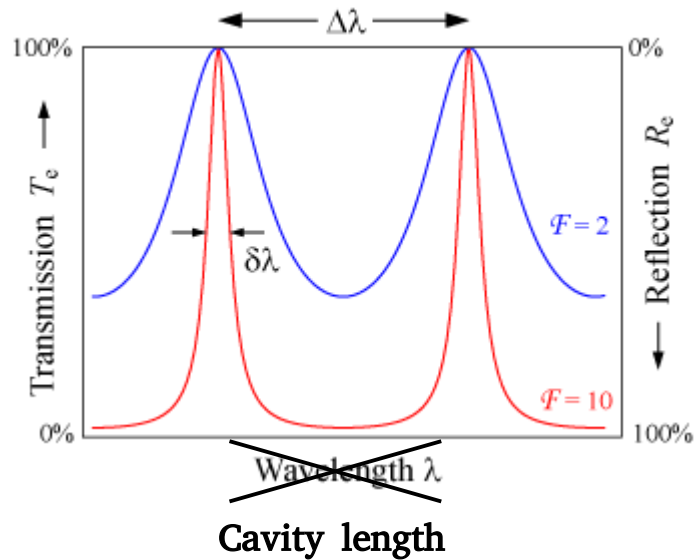
Lock control

The detector's mirrors must be "controlled" to lock and maintain the cavities at resonance



Lock control

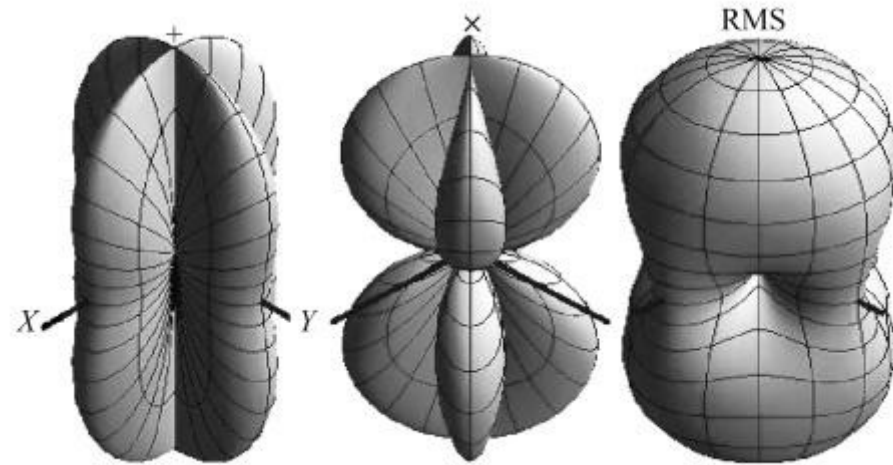
The detector's mirrors must be "controlled" to lock and maintain the cavities at resonance



A control loop is activated to bring (and maintain) the mirrors at resonance

Sky coverage

The detector's sensitivity over the sky is not uniform



$$h_{det}(t) = F_{+}(t, \underline{ra}, \underline{dec}, \underline{\Psi}) \times h_{+}(t) + F_{\times}(t, \underline{ra}, \underline{dec}, \underline{\Psi}) \times h_{\times}(t)$$

Source position Source polarization angle

Power spectral density

Fourier transform

A time series $s(t)$ can be projected over a basis of sinusoidal functions:

$$\tilde{s}(f) = \int_{-\infty}^{\infty} s(t) e^{-2i\pi ft} dt \quad (\text{forward})$$

$$s(t) = \int_{-\infty}^{\infty} \tilde{s}(f) e^{2i\pi ft} df \quad (\text{backward})$$

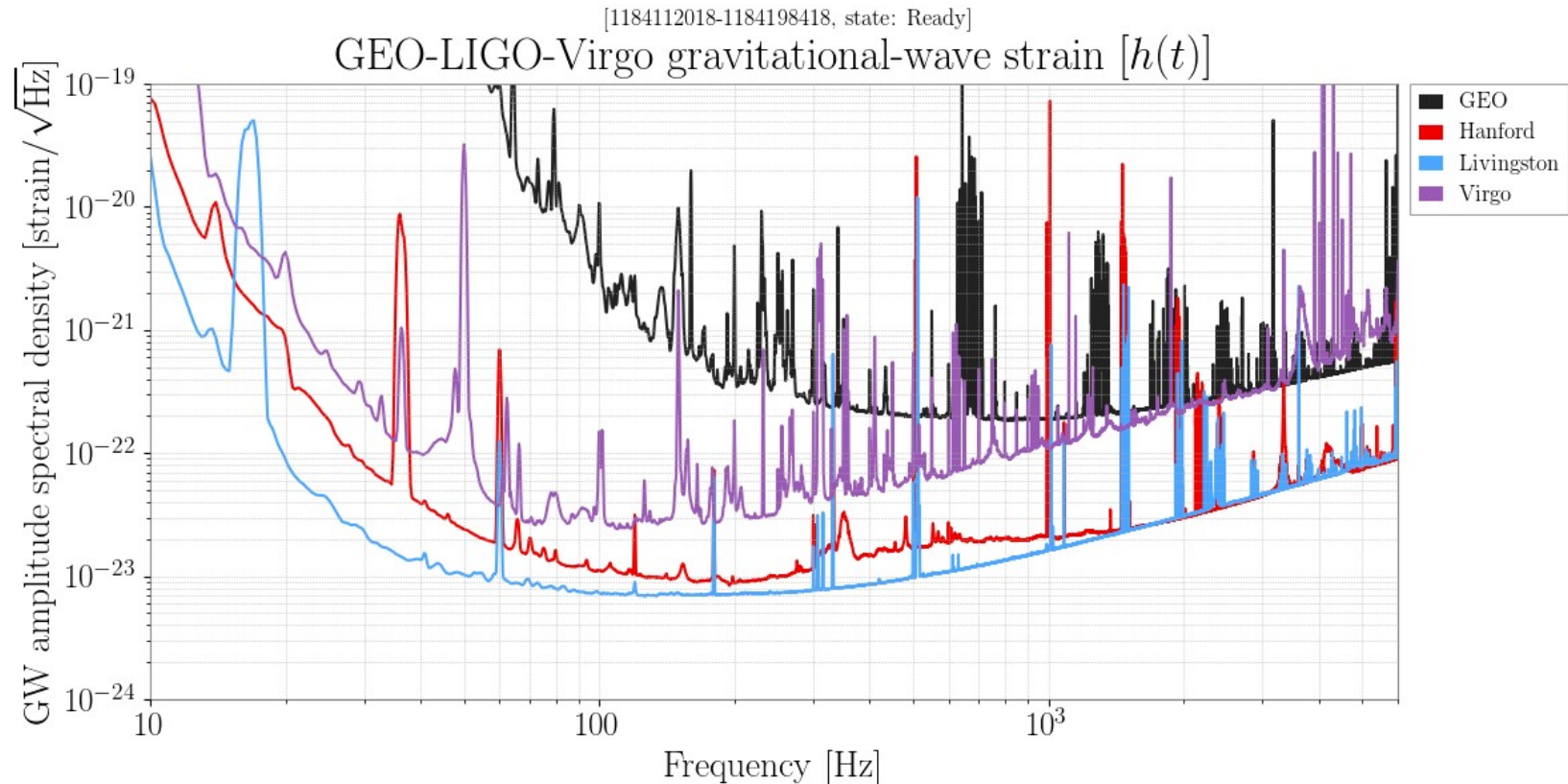
The signal is decomposed in characteristic frequencies

A noise source $n(t)$ limiting the extraction of a signal $s(t)$ is completely characterized by the power (amplitude) spectral density $S_n(f)$

$$S_n(f) = 2|\tilde{n}(f)|^2 \quad A_n(f) = \sqrt{S_n(f)}$$

Detector sensitivity

LIGO-Virgo sensitivity – 2017

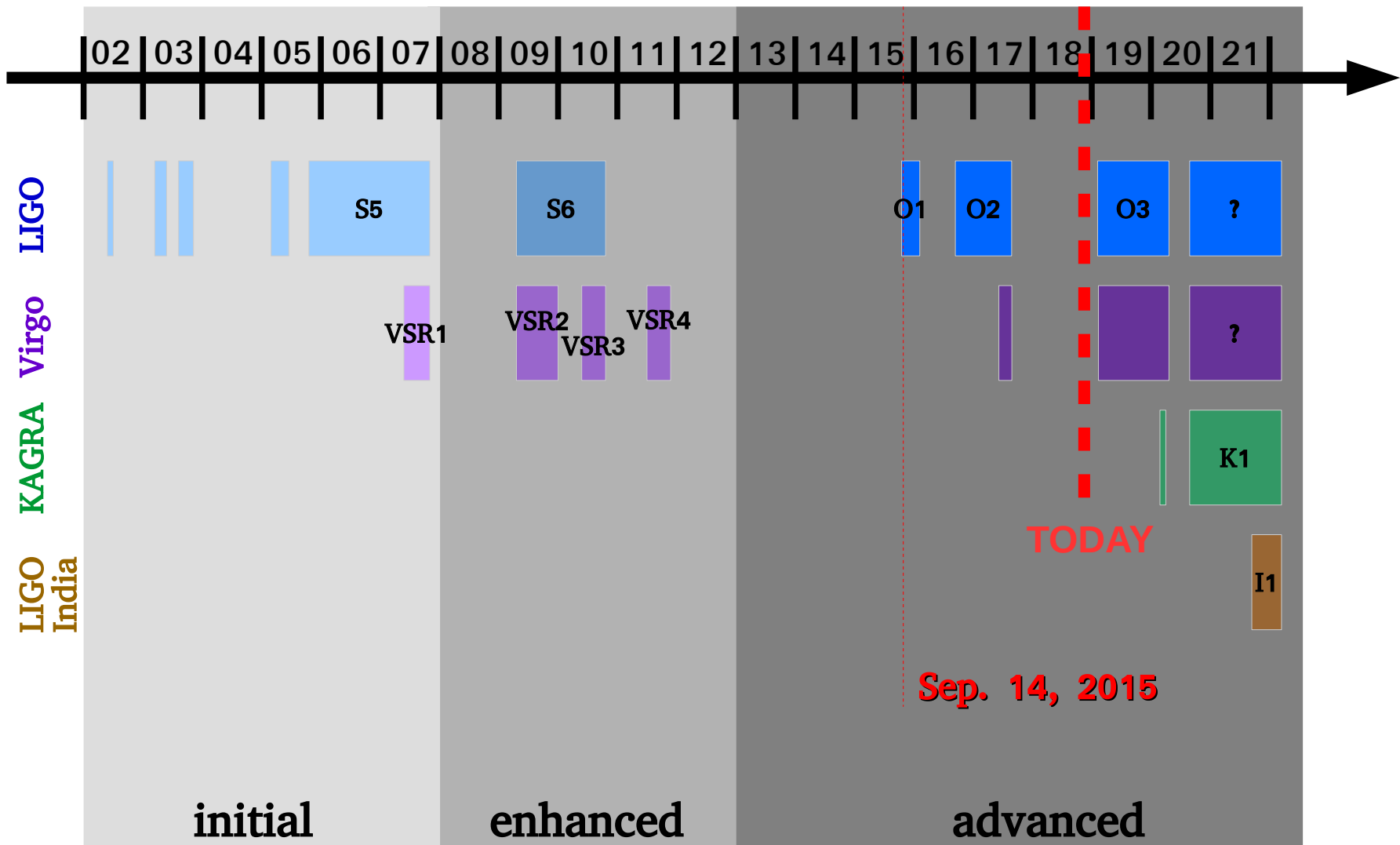


Fundamental noises:

- $f < 10$ Hz → seismic noise
- 10 Hz $< f < 200$ Hz → thermal noise
- $f > 200$ Hz → quantum shot noise

+ technical noise (environment, scattered light, control...)

Scientific runs



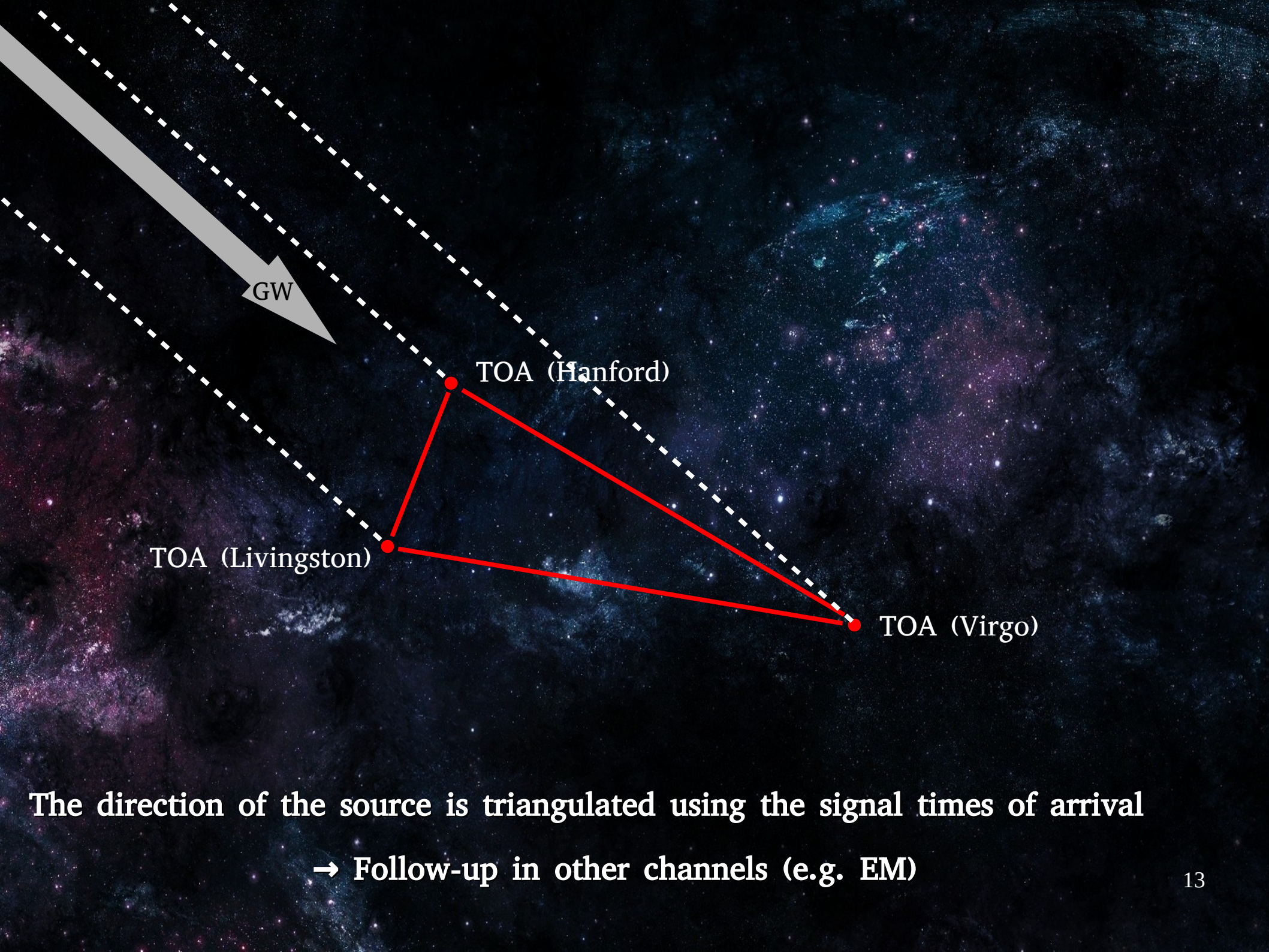
Data analysis :

- O1 : ~50 days of data, 2 detectors
- O2 : ~100 days of data, 2(+1) detectors
- O3 : ~200 days of data, 3 detectors

Working with a network of detectors is mandatory

- to perform a coincident search
- to test the signal consistency across the network
- to estimate your background noise
- to locate the source of gravitational waves





GW

TOA (Hanford)

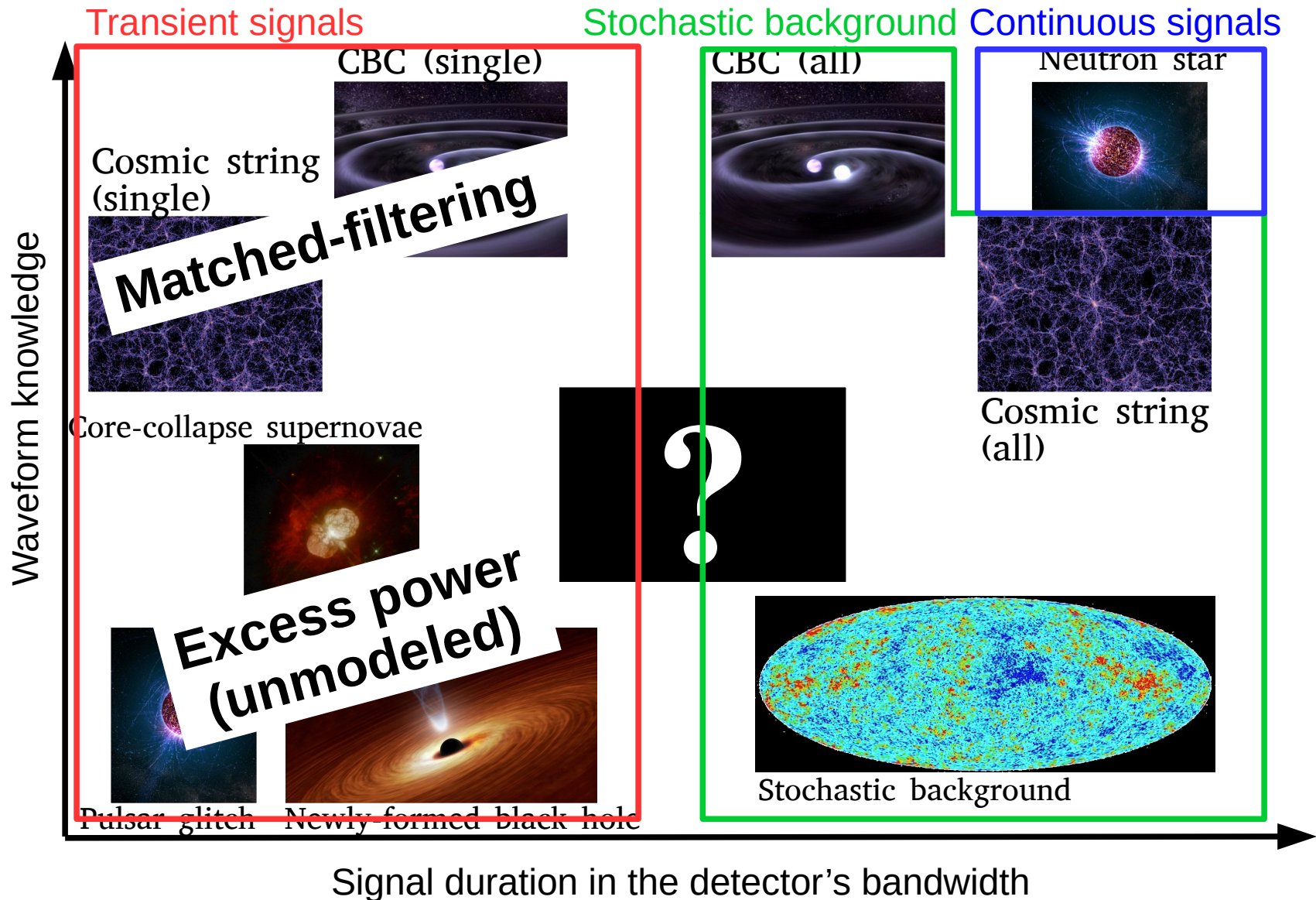
TOA (Livingston)

TOA (Virgo)

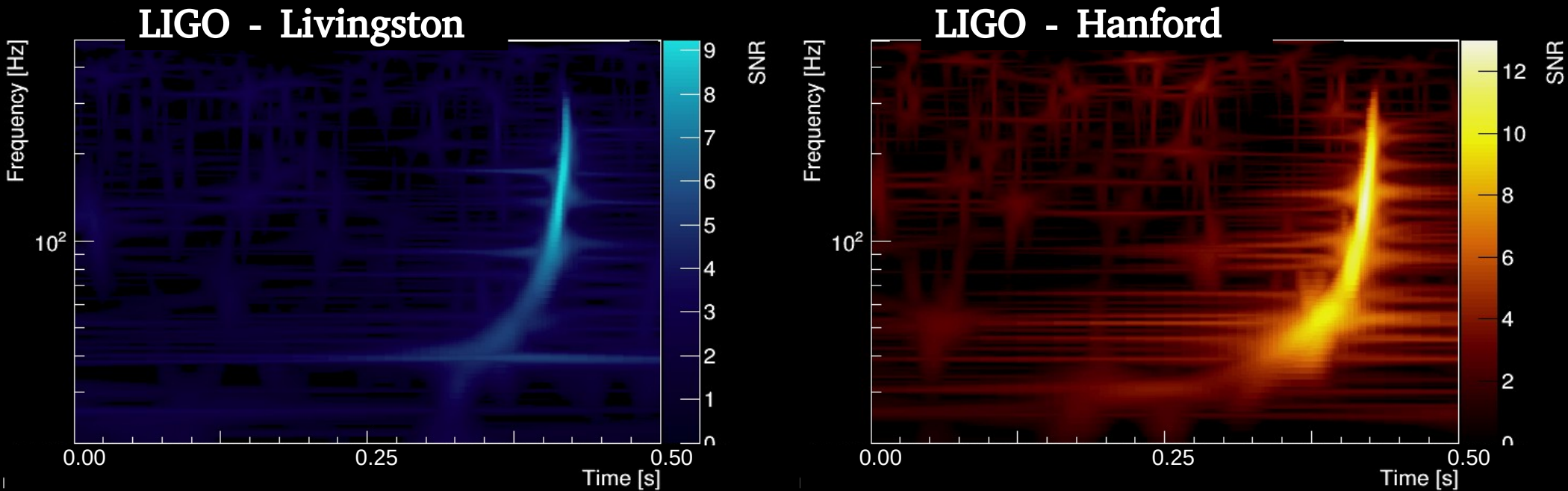
The direction of the source is triangulated using the signal times of arrival

→ Follow-up in other channels (e.g. EM)

Source classification: search method



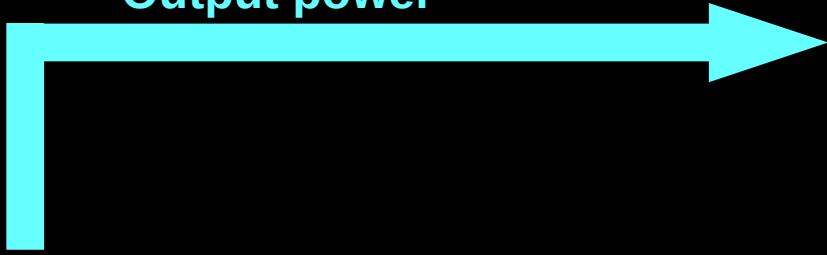
Unmodeled searches



- Time-frequency decomposition → noise events + (maybe) GW events
- Coincidence between detectors (time + other parameters)
- Noise rejection
- Classify events using a “smart” recipe
- Estimate background
- Compare events with your background
- Measure the probability for each events to be true GW signal

GW150914

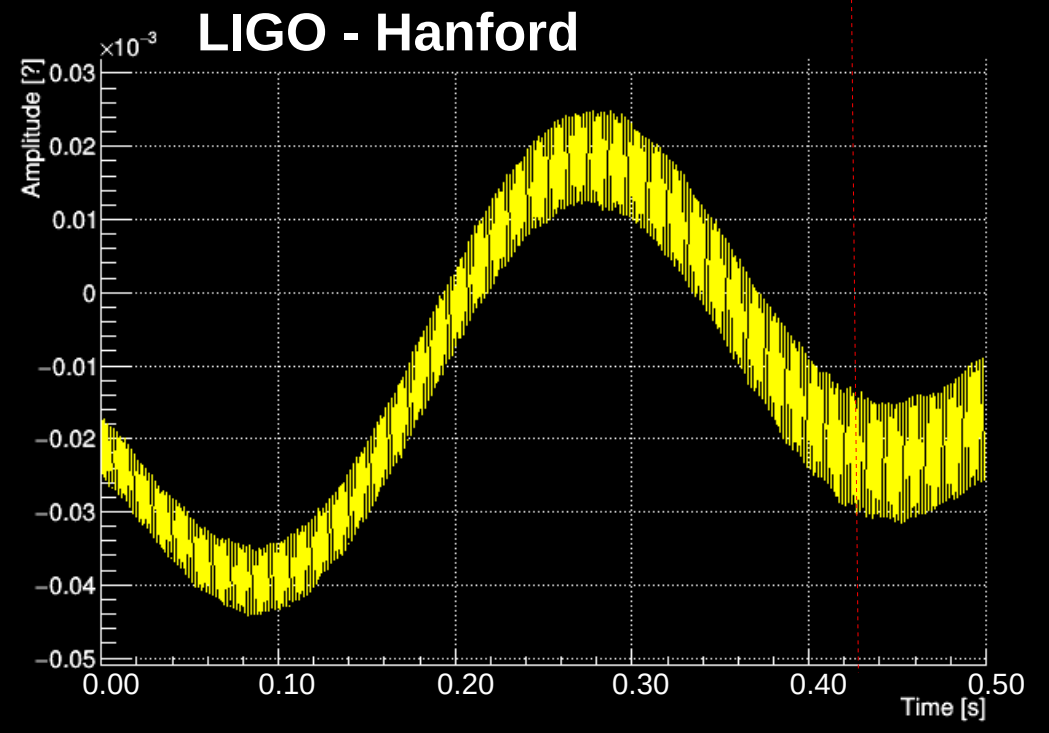
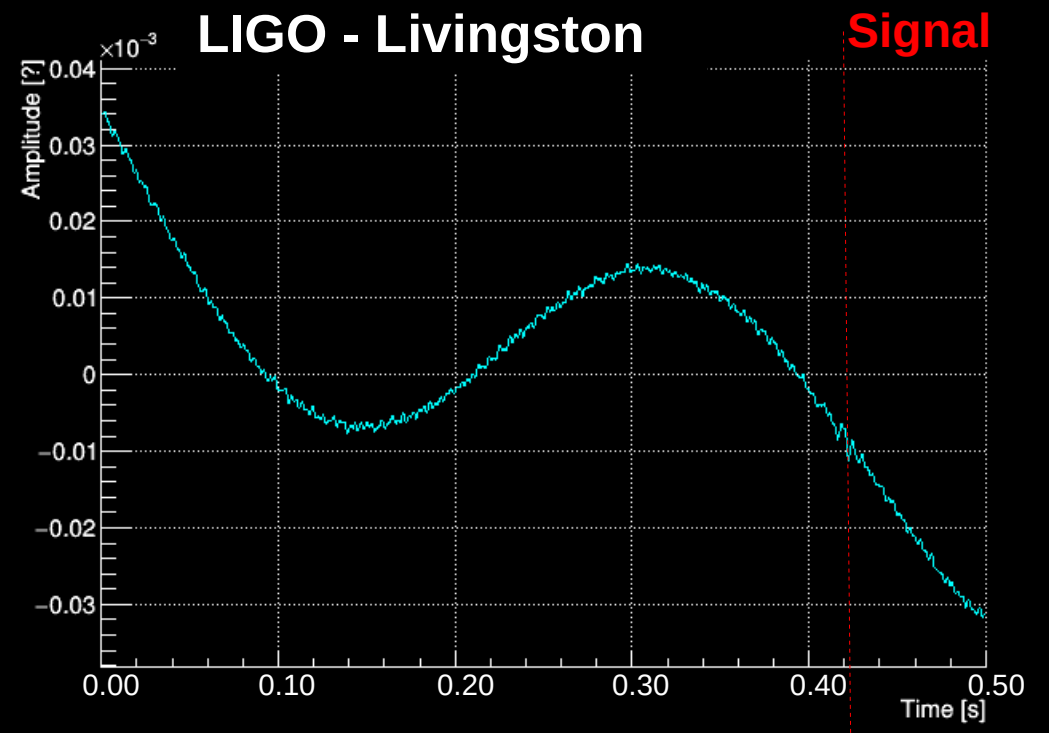
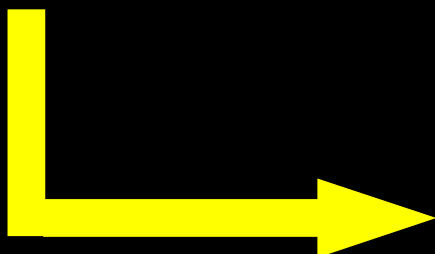
Output power



Livingston

Hanford

Output power

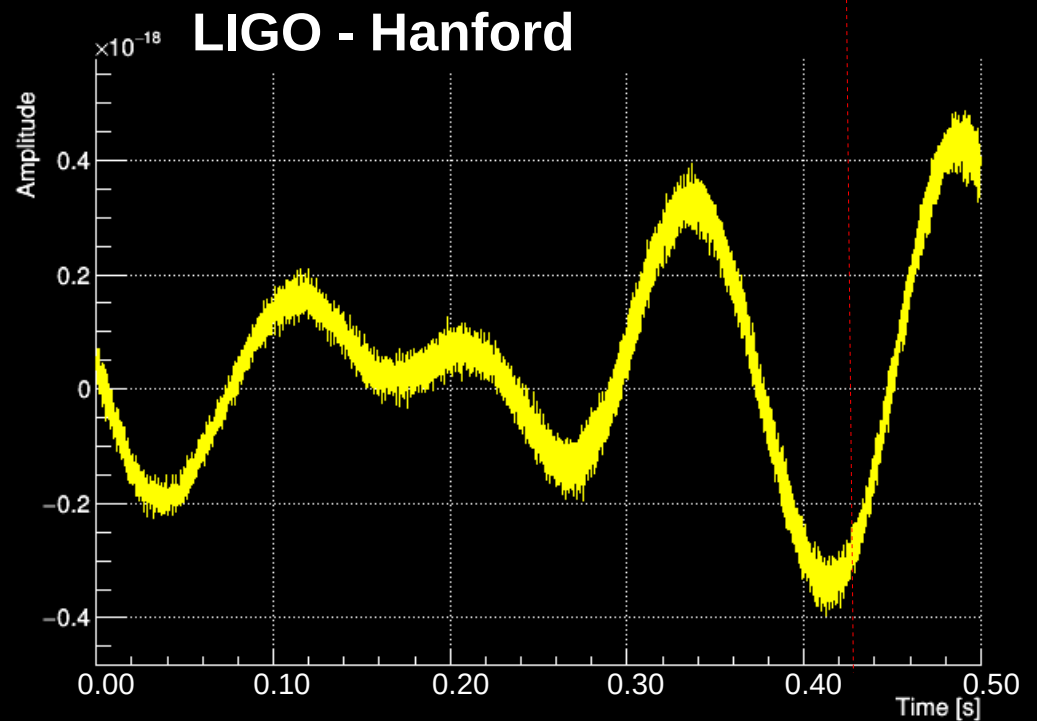
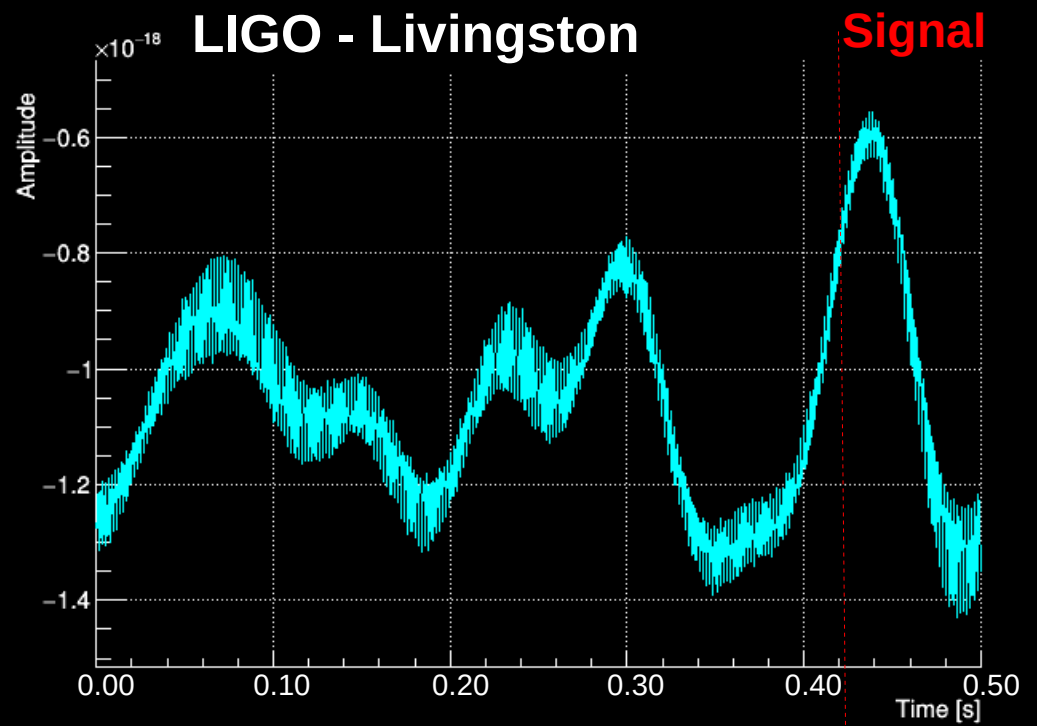


GW150914

$$h(t)$$

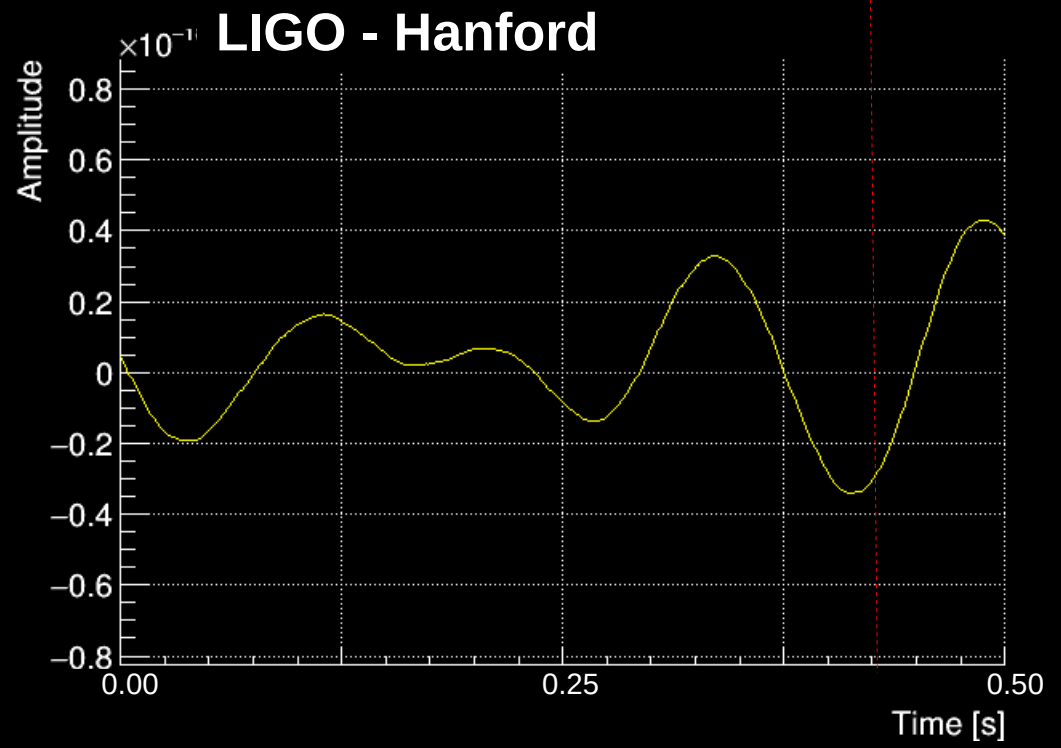
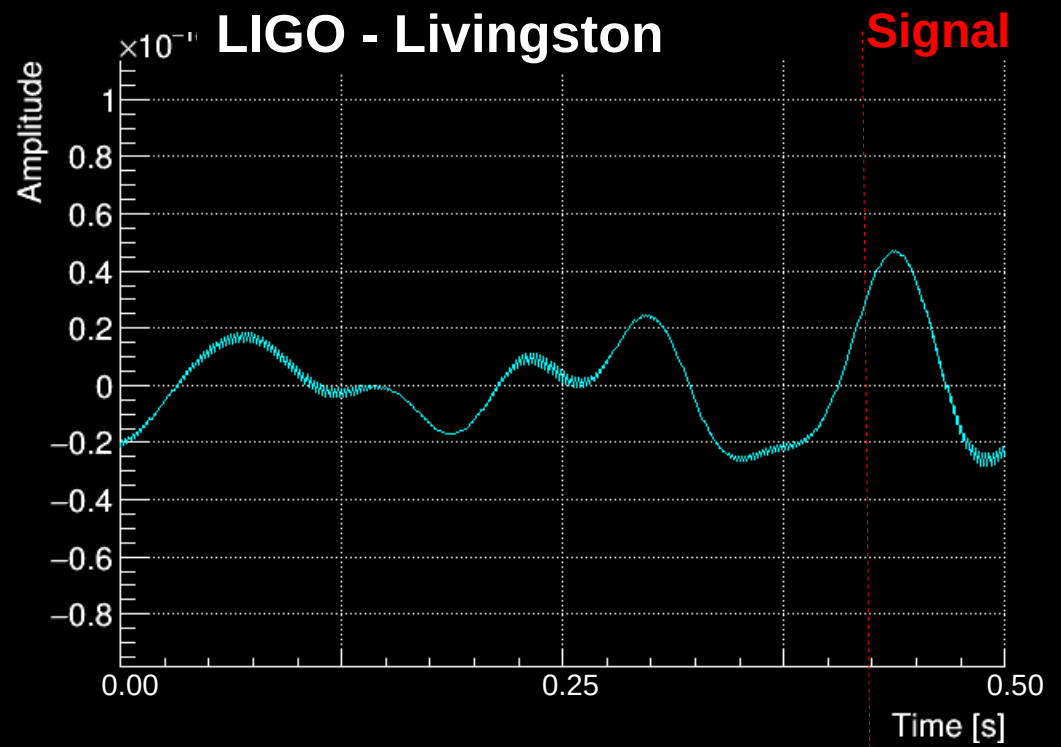
Data is calibrated

→ GW strain amplitude $h(t)$
(including high-pass filter $f > 10$ Hz)



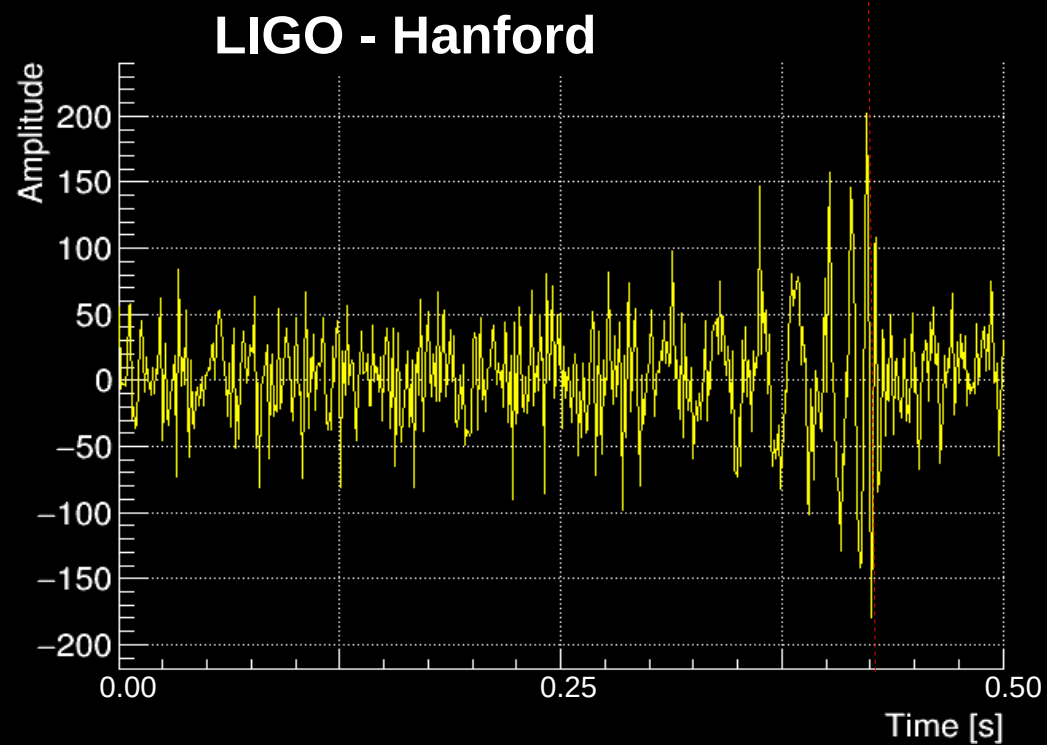
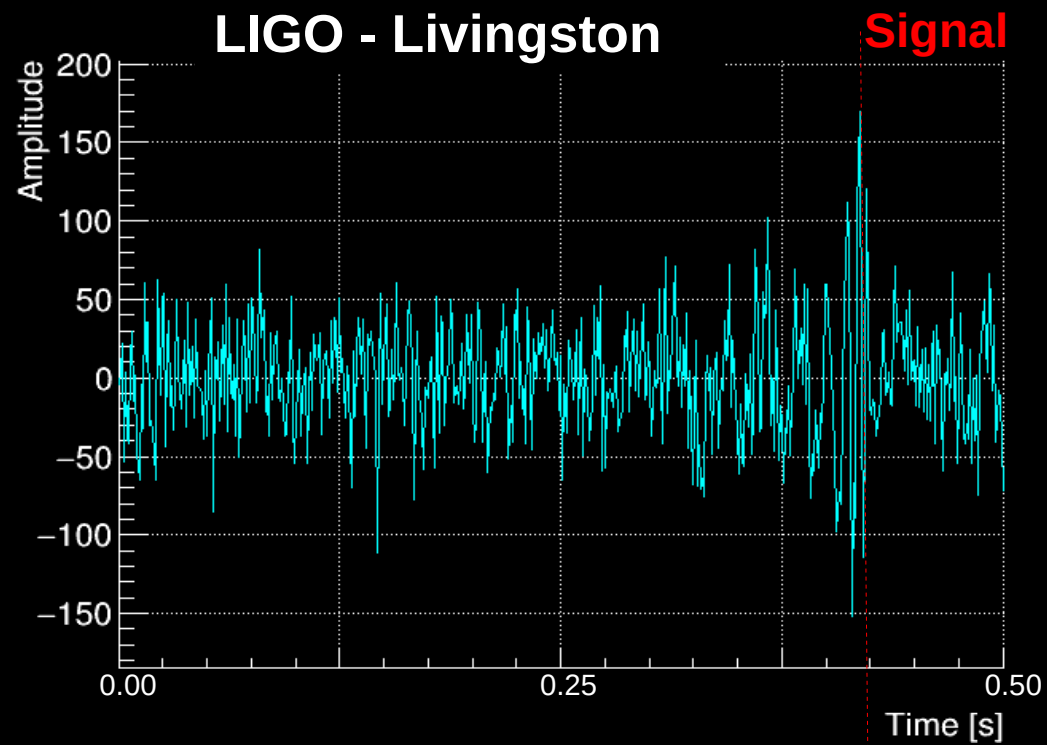
GW150914

Data are low-pass filtered
(here, < 500 Hz)



GW150914

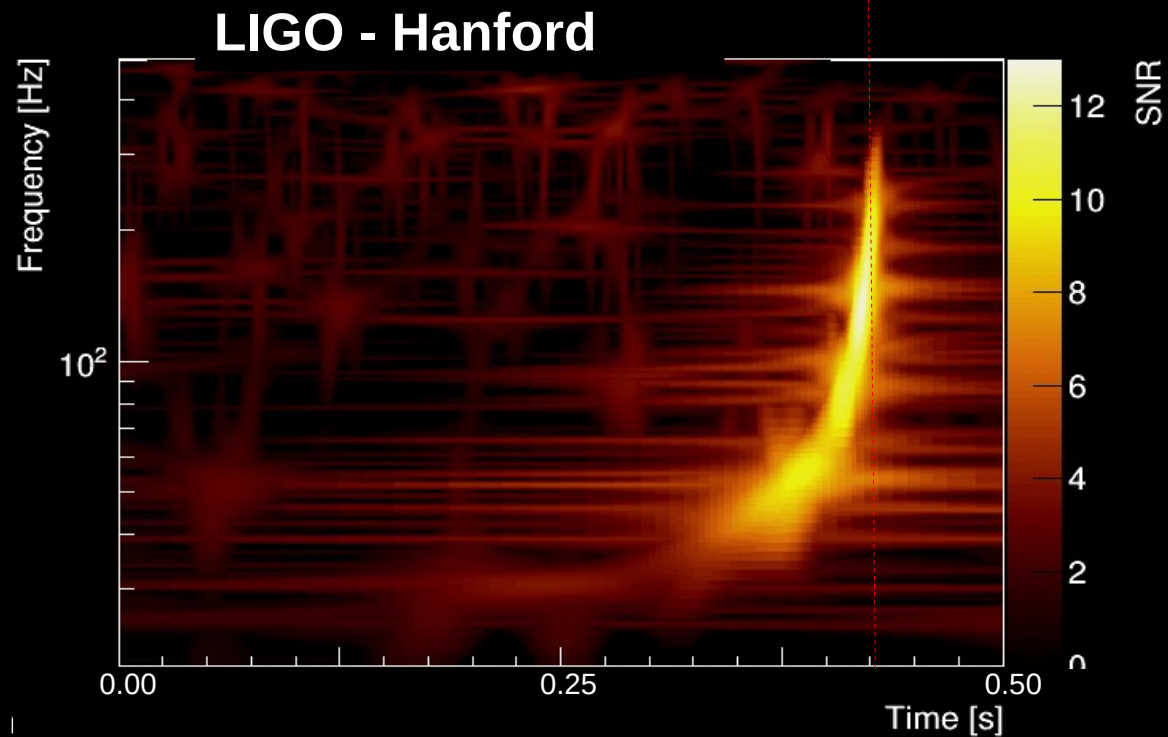
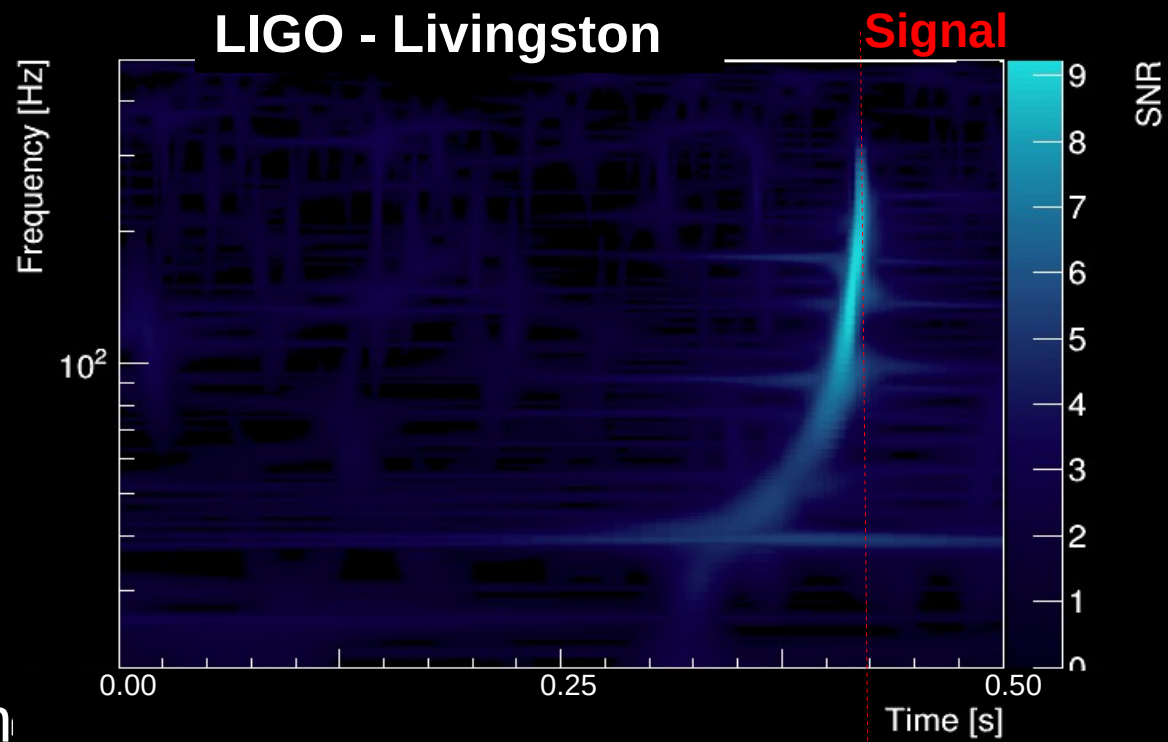
Data are whitened



GW150914

Time-frequency decomposition
(Short Fourier transforms)

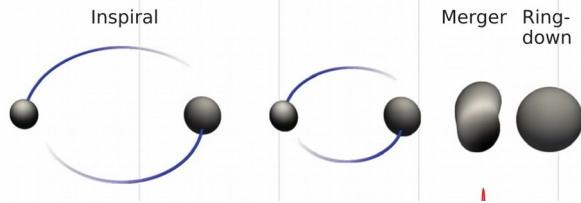
$$X(\tau, \phi, Q) = \int_{-\infty}^{+\infty} h_{det}(t) w(t - \tau, \phi, Q) e^{-2i\pi\phi\tau} dt$$



Modeled search

Theoretical input:

- 90s: CBC PN waveforms (Blanchet, Iyer, Damour, Deruelle, Will, Wiseman, ...)
- 00s: CBC Effective One Body “EOB” (Damour, Buonanno)
- 06: BBH numerical simulation (Pretorius, Baker, Loustos, Campanelli)



The intrinsic waveform parameters:

- Masses:

$$M_{tot} = M_1 + M_2$$

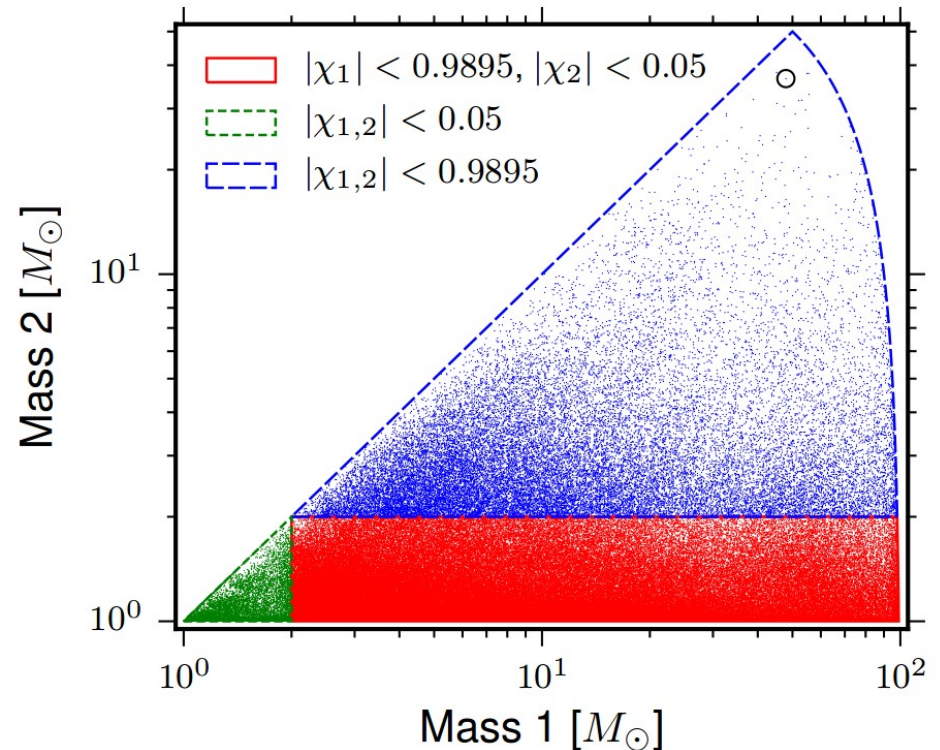
- Spins and orbital angular momentum:

$$\vec{S}_{tot} = \vec{S}_1 + \vec{S}_2 + \vec{J}$$

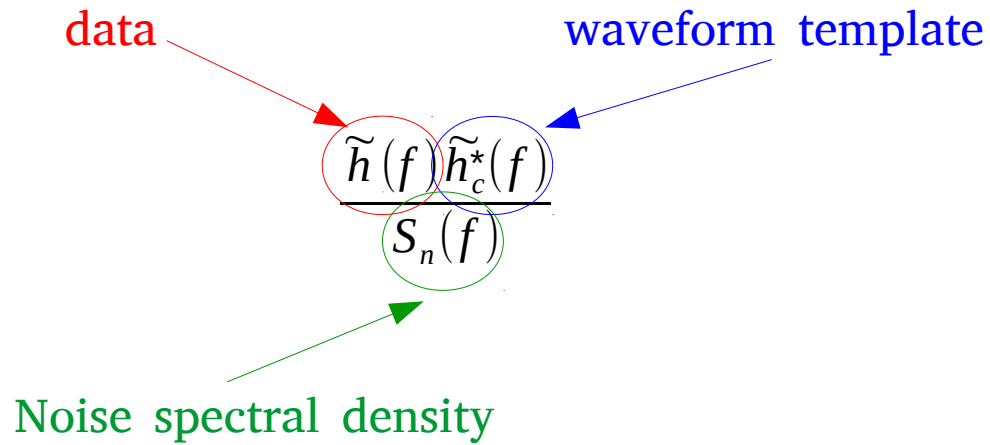
The waveform models used for the search:

- Inspiral, PN3.5 for $M_{tot} < 4 M_{sun}$
- Inspiral/Merger/Ringdown EOB + numerical relativity for $M_{tot} > 4 M_{sun}$
- Spins and orbital angular momentum are aligned

Template bank → match-filtering technique



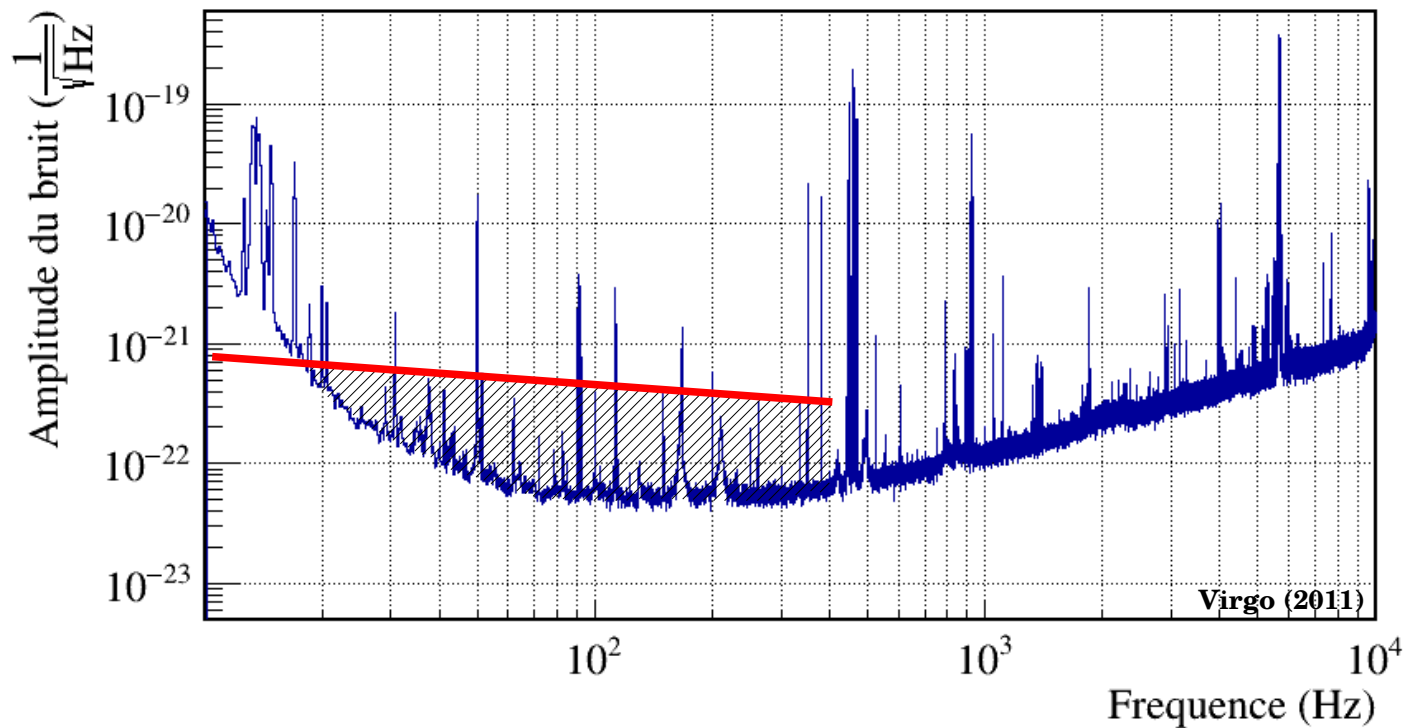
Match filtering



Match filtering

$$\rho_c(t) = 4 \Re \left[\int_0^\infty \frac{\tilde{h}(f) \tilde{h}_c^*(f)}{S_n(f)} e^{2i\pi f t} df \right]$$

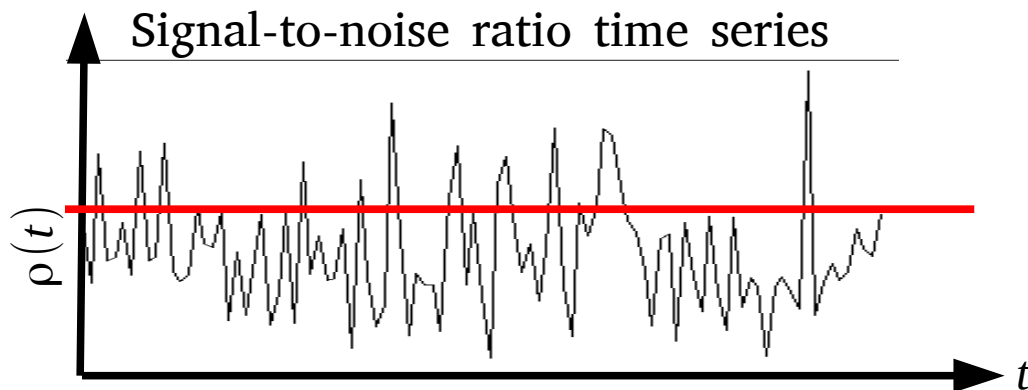
A signal-to-noise ratio (SNR) is computed for each template



Match filtering

$$\rho_c(t) = 4 \Re \left[\int_0^\infty \frac{\tilde{h}(f) \tilde{h}_c^*(f)}{S_n(f)} e^{2i\pi f t} df \right]$$

A signal-to-noise ratio (SNR) is computed for each template



A list of events is produced:

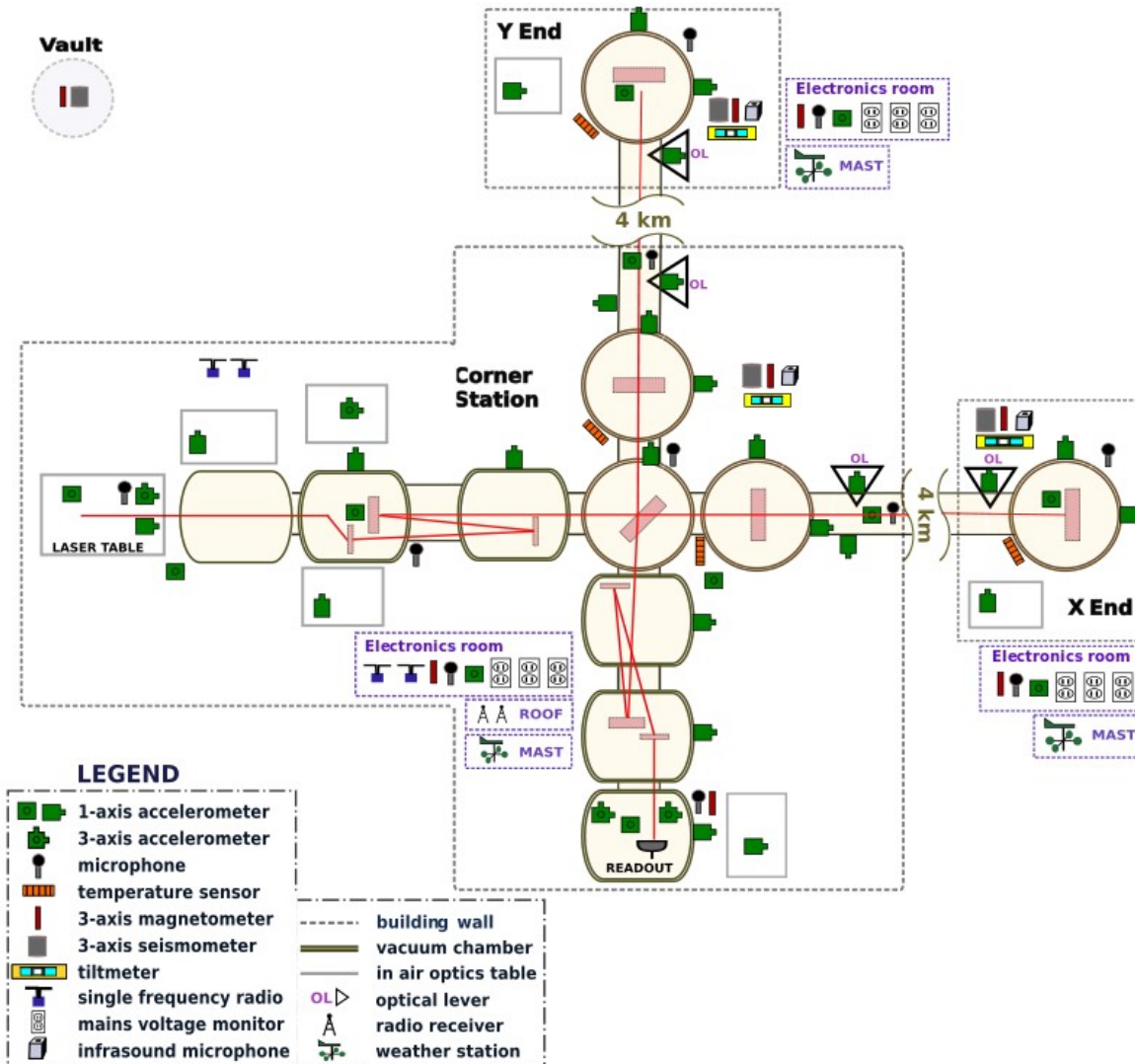
- start/end/peak times
- SNR
- template parameters (masses, spins)

Now the challenge is to reject noise events to better isolate true signals

Monitoring noise

Thousands of auxiliary channels are used to monitor the instruments

- environmental sensors
- detector sub-systems
- detector control

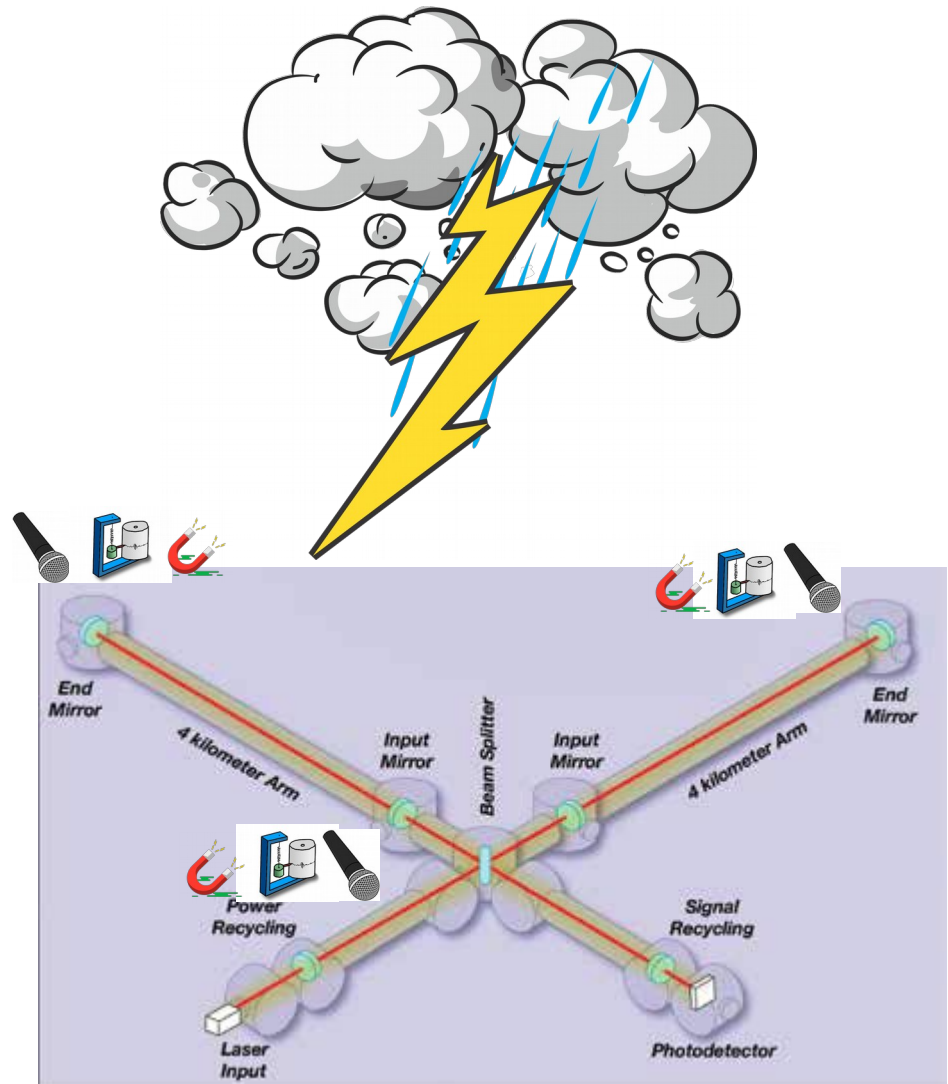
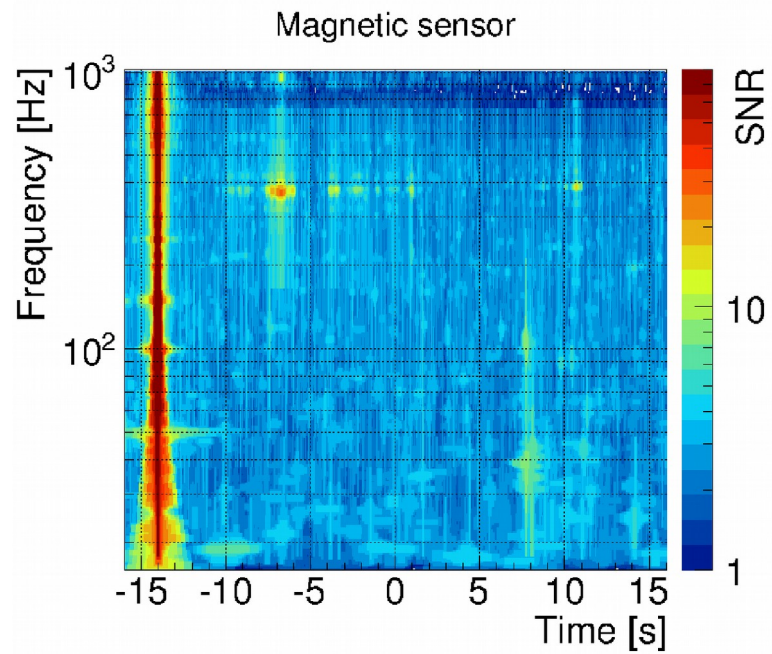
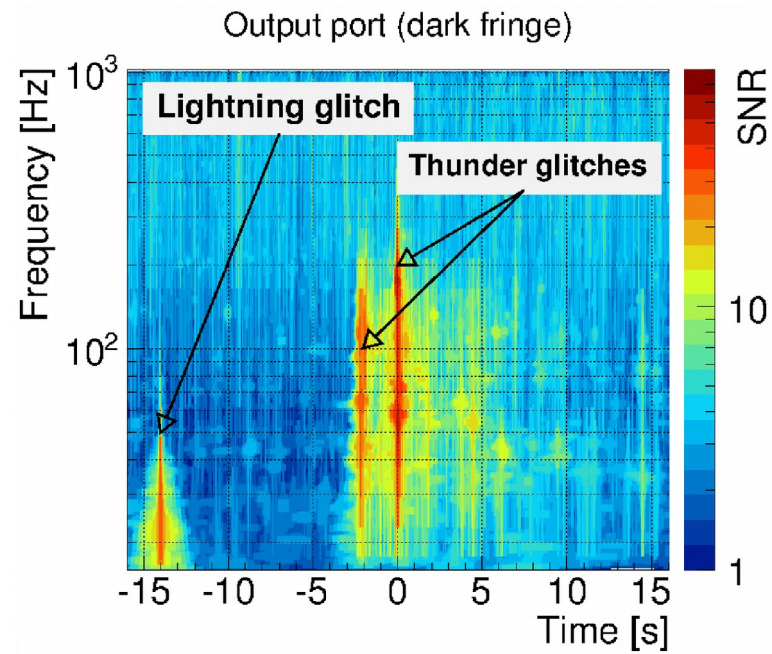


Noise injection campaigns are conducted to identify the detector's response to different noise stimulation

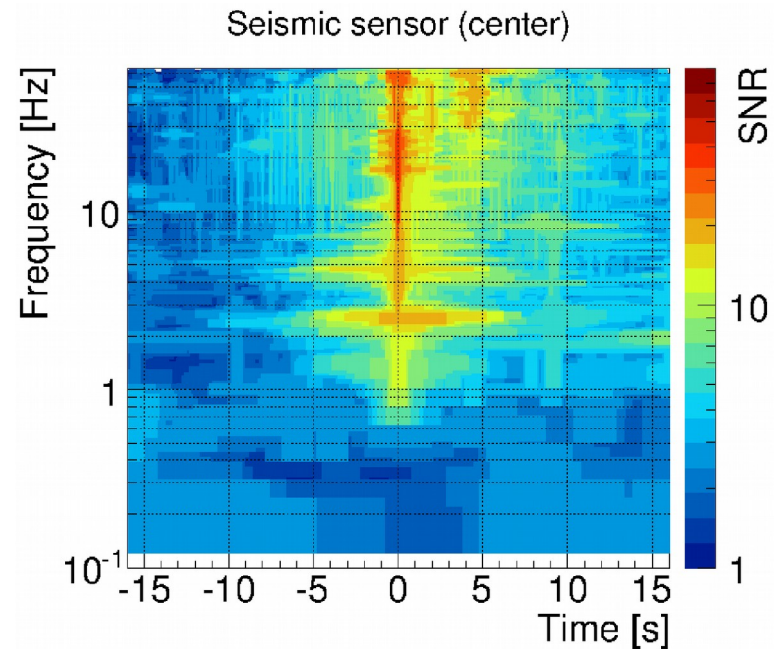
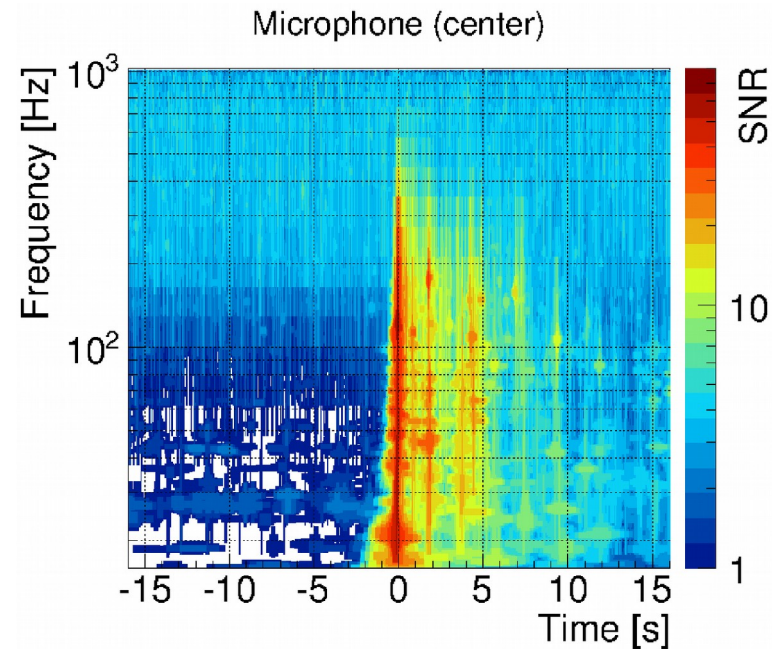
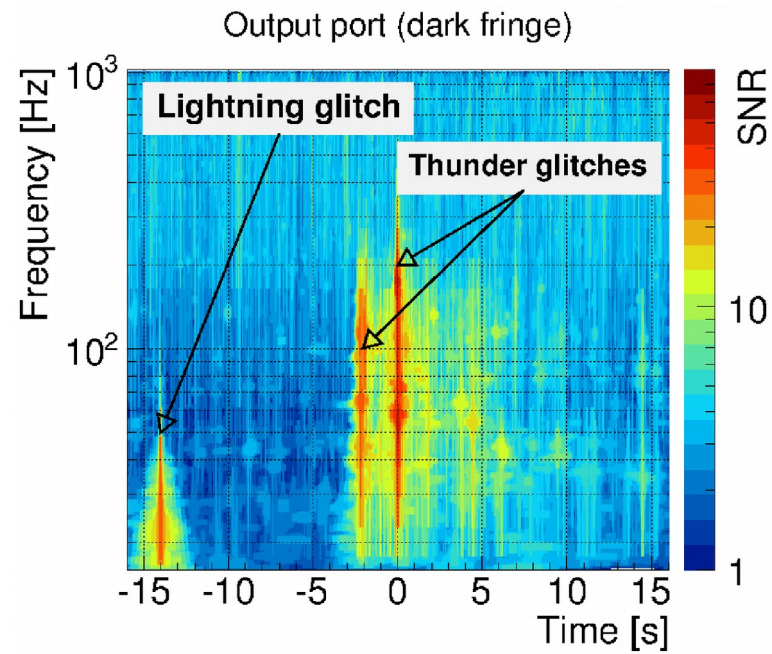
- Multiple transient noises were identified during the run
- Anthropogenic noise
 - Earthquakes
 - Radio-frequency modulation
 - ...

- Option #1: fix the detector
- Option #2: remove transient events in the data

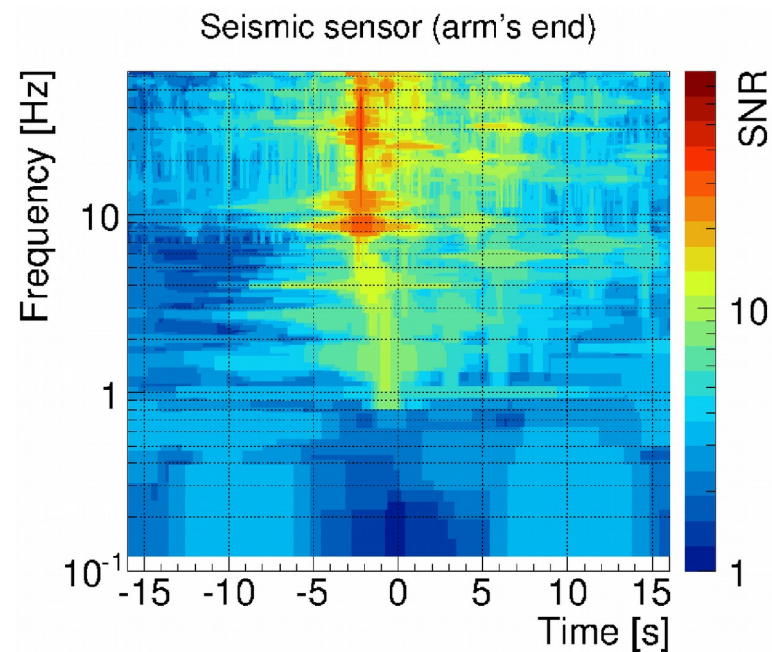
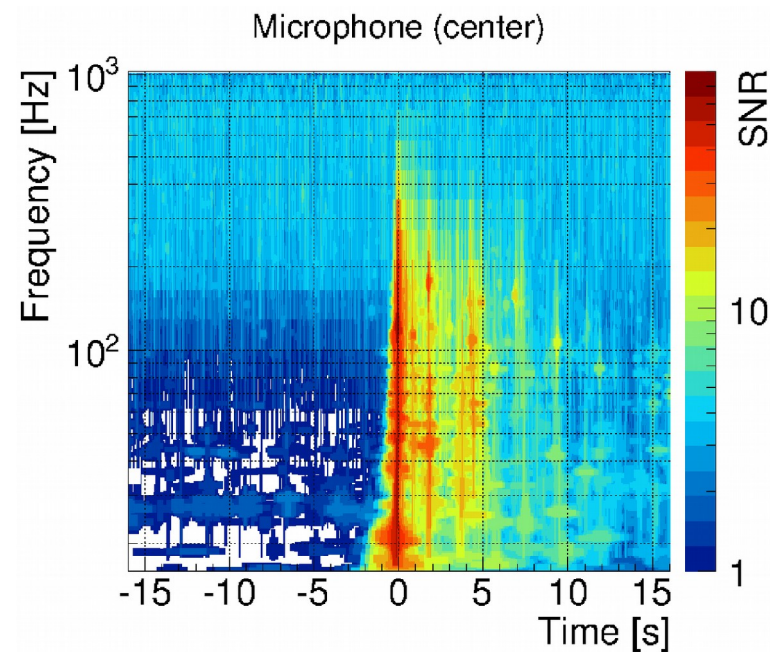
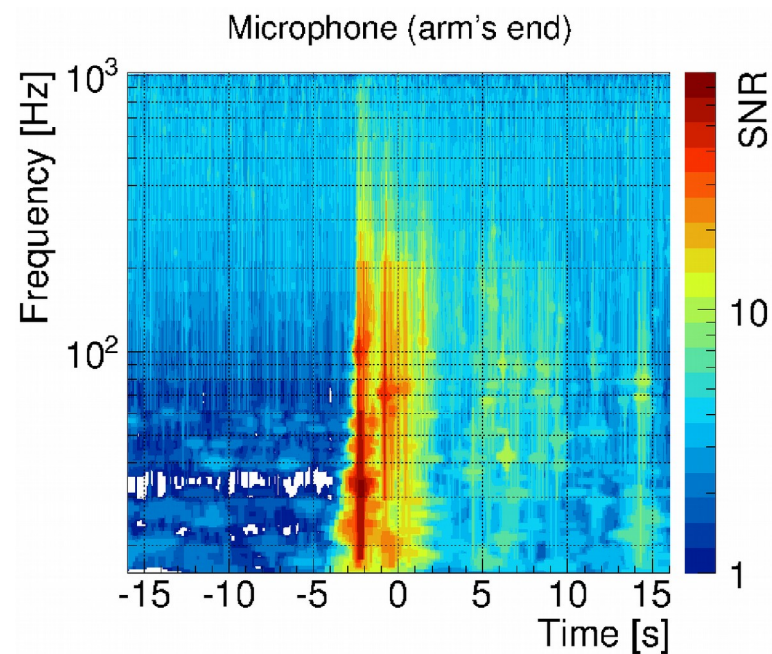
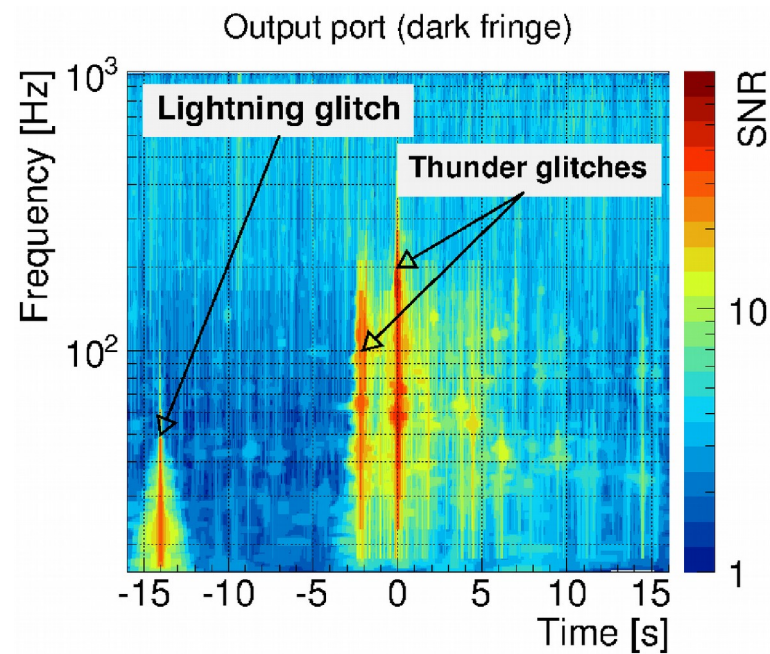
Monitoring noise



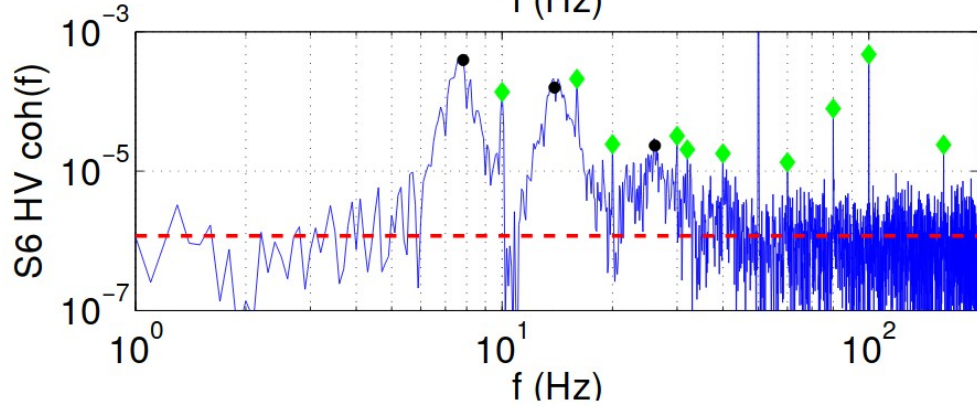
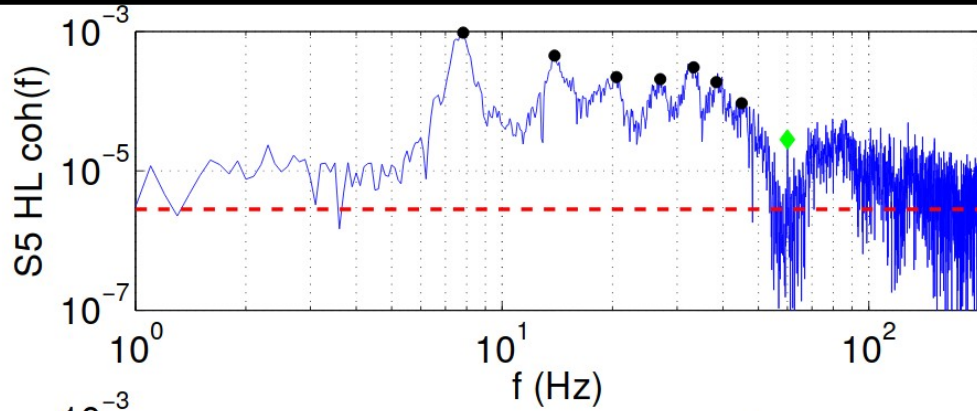
Monitoring noise



Monitoring noise



Correlated noise

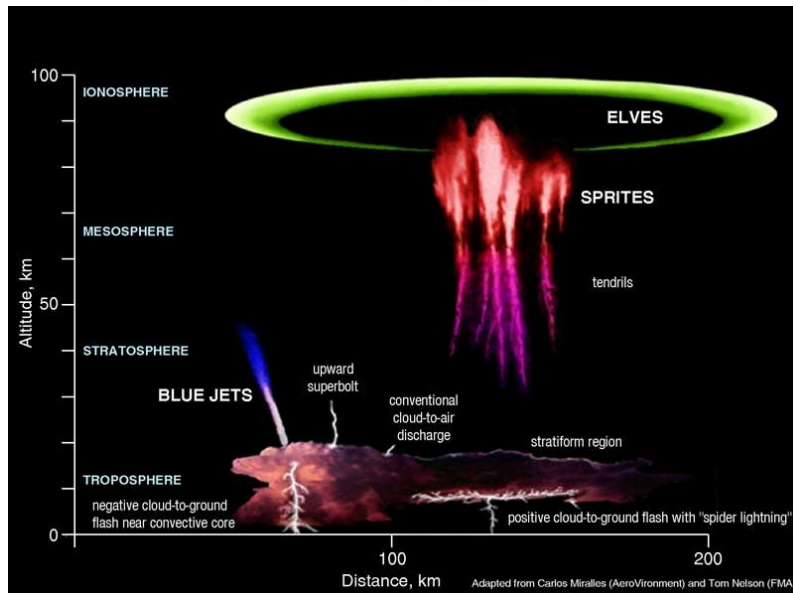
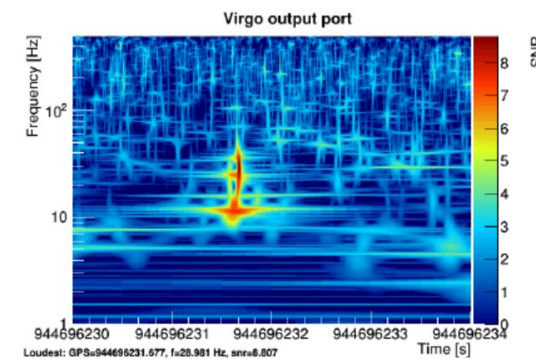
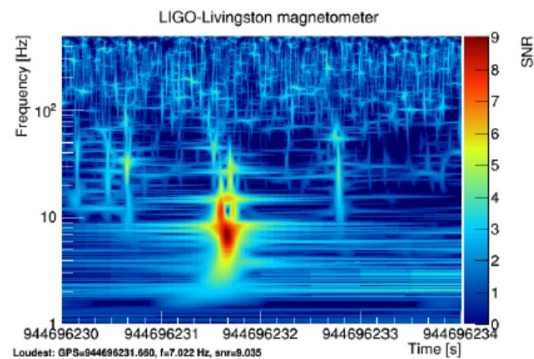
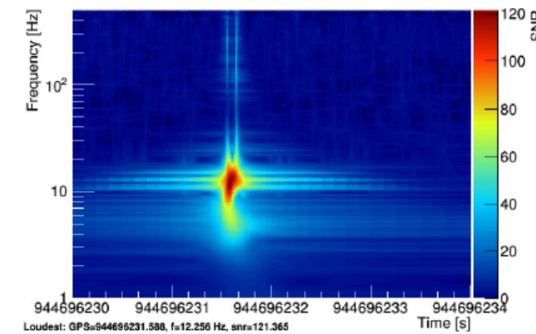
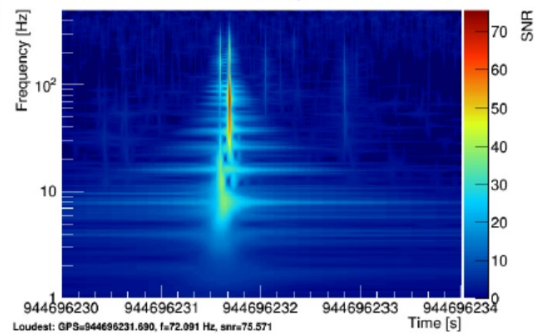


Schumann resonance



LIGO-Hanford magnetometer

Virgo magnetometer



Adapted from Carlos Miralles (AeroVironment) and Tom Nelson (FMA)

Conclusions

- First detection achieved by ground-based interferometers (LIGO-Virgo)
- A network of detectors is needed
 - to detect a gravitational-wave with confidence
 - to localize the source
 - to estimate the parameters of the source
- Analysis pipelines are used to analyze the data
- Gravitational-wave detectors are very sensitive instruments
- Multiple noise sources