



November 10-16, 2018 An-Najah N. University, Nablus, Palestine

# Multi-messenger astronomy and cosmology

→ Lecture 1 Introduction to gravitational waves

→ Lecture 2 Detection of gravitational waves

→ Lecture 3 Multi-messenger astronomy

→ Lecture 4 Observational cosmology



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# Introduction to gravitational waves

- → General relativity
- → Gravitational waves
- $\rightarrow$  First detections of gravitational waves
- → Characterization of black hole binary systems



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- ▶ 1915: The theory of general relativity is published by Albert Einstein
- Current description of gravitation
- Superior to Newtonian gravity
- ➤ Gravity = geometric description of space and time



Metric: space-time structure, used to define distances Space-time is described by the metric tensor  $g_{\mu\nu}$ 

Distances are measured by integrating the distance element:  $ds^2 = g_{\mu\nu} dx^{\mu} dx^{\nu}$ 

Example: Minkowski flat metric (empty space, c=1)

$$g_{\mu\nu} = \eta_{\mu\nu} = \begin{pmatrix} -1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{pmatrix}$$

$$ds^{2} = -dx^{0} dx^{0} + dx^{1} dx^{1} + dx^{2} dx^{2} + dx^{3} dx^{3}$$
Euclidean metric
In presence of gravity, the metric is curved
$$\rightarrow \text{ distance = geodesics}$$

Einstein's equation:

$$G_{\mu\nu} = R_{\mu\nu} - \frac{1}{2} g_{\mu\nu} R(+\Lambda g_{\mu\nu}) = \frac{8 \pi G}{c^4} T_{\mu\nu}$$

Space-time curvature Mass/energy

 $R_{\mu\nu} = R^{\alpha}_{\ \mu\alpha\nu}$  Ricci tensor = contraction of Riemann tensor

- $R = R^{\alpha}_{\alpha}$  Scalar curvature: Ricci tensor contraction
- $T_{\mu\nu}$  Energy-momentum tensor: density and flux of energy and momentum

The entire theory is encoded in a single expression!

- > Symmetrical tensors  $\rightarrow$  10 equations
- Highly non-linear equations



#### Predictions of the theory

- Anomalous shift (43") of the Mercury perihelion
- Light deflection by gravity (observed in 1919)
- Gravitational redshift (observed in 1959)
- Gravitational lensing (observed in 1979)
- Black holes (observed indirectly)
- Gravitational waves (observed in 2015!)



# Black holes

Region of space-time deformed by a compact mass from which nothing can escape (not even light). Introduced by Schwarzschild in 1916

Escape velocity (Newton): 
$$v_e = \sqrt{2 \frac{Gm}{r}}$$
  $v_e = c$   $R_s = 2 \frac{Gm}{c^2}$  Schwarzschild radius  
Black hole:  $R < R_s = 2 \frac{Gm}{c^2}$ 

Earth	Sun	Neutron star	Black hole	
$R_s = 9 mm$	$R_s = 3  km$	$R_s \sim 5 \ km$	$R_s \sim 10 \ km$	Composity
R = 6000  km	R = 700000km	$R \sim 10  km$	$R < R_s$	Compacity

7

# Black holes

Theoretical developments in the 60s:

- Rotating black hole solution (Kerr, 1963)
- Electrically charged black hole (Newman, 1965)
- No-hair theorem: mass+spin+charge (1967)
- Singularities as generic solutions (Hawking/Penrose, 1969)
- > Stellar black hole = result from the collapse of a massive star (m = 3-100  $M_{sun}$ )
- > Supermassive black hole = low-density object at the center of a galaxy (m  $\sim 10^9$  M<sub>sun</sub>)
- > Primordial black hole = extremely dense object formed just after the big-bang.



Observational evidence:

- star motion near the Milky Way center

- accretion of matter on black holes = bright X-ray sources (X-ray binaries, quasars, AGN)

→ *indirect* observations

688 Sitzung der physikalisch-mathematischen Klasse vom 22. Juni 1916

#### Näherungsweise Integration der Feldgleichungen der Gravitation.

Von A. EINSTEIN.



Bei der Behandlung der meisten speziellen (nicht prinzipiellen) Probleme auf dem Gebiete der Gravitationstheorie kann man sich damit begnügen, die  $g_{a}$ , in erster Näherung zu berechnen. Dabei bedient man sich mit Vorteil der imaginären Zeitvariable  $x_{4} = it$  aus denselben Gründen wie in der speziellen Relativitätstheorie. Unter verster Näherung« ist dabei verstanden, daß die durch die Gleichung

$$g_{ar} = -\delta_{ar} + \gamma_{ar}$$

(1)

definierten Größen  $\gamma_{\mu\nu}$ , welche linearen orthogonalen Transformationen gegenüber Tensorcharakter besitzen, gegen 1 als kleine Größen behandelt werden können, deren Quadrate und Produkte gegen die ersten Potenzen vernachlässigt werden dürfen. Dabei ist  $\delta_{\mu\nu} = 1$  bzw.  $\delta_{\mu\nu} = 0$ , je nachdem  $\mu = \nu$  oder  $\mu \neq \nu$ .

Wir werden zeigen, daß diese y" in analoger Weise berechnet werden können wie die retardierten Potentiale der Elektrodynamik.

small perturbation of Minkowski's metric

$$G_{\mu\nu} = R_{\mu\nu} - \frac{1}{2} g_{\mu\nu} R = \frac{8 \pi G}{c^4} T_{\mu\nu} = 0$$

Add a small perturbation to a flat metric:  $g_{\mu\nu} = \eta_{\mu\nu} + h_{\mu\nu} \qquad |h_{\mu\nu}| \ll 1$ 

Einstein equations can be linearized and solved: *h* obeys a plane-wave equation (transverse-traceless gauge)
the wave propagates at the speed of light
2 degrees of freedom: *h*<sub>+</sub> and *h*<sub>x</sub>

#### → Gravitational waves



# Gravitational-wave emission



Quadrupole (traceless)  $Q_{ii} = \int \rho(x_i x_i) d^3 \vec{r}$ 

Einstein quadrupole formula (radiated power)

 $\sim$ 

$$\frac{dE}{dt} = -\frac{G}{5c^5} \left\langle \frac{d^3Q^{ij}}{dt^3} \frac{d^3Q_{ij}}{dt^3} \right\rangle$$

Estimate using the source parameters  $Q \sim \varepsilon M R^2$ 

$$\frac{d^3Q}{dt^3} \sim \varepsilon M R^2 \omega^3$$

$$\frac{dE}{dt} \sim -\frac{G}{c^5} \varepsilon^2 M^2 R^4 \omega^6 \sim -\frac{c^5}{G} \varepsilon^2 \left(\frac{R_s}{R}\right)^2 \left(\frac{v}{c}\right)^6$$
$$\simeq 10^{52} W$$

- $\rightarrow$  Important source characteristics:
- asymmetric
- compact
- relativistic

## Gravitational-wave sources



# Gravitational-wave emission



z projection in transverse-traceless gauge:

$$\ddot{Q} = \begin{pmatrix} -4 ma^2 \omega^2 \cos(2\omega t) & -4 ma^2 \omega^2 \sin(2\omega t) \\ -4 ma^2 \omega^2 \sin(2\omega t) & 4 ma^2 \cos(2\omega t) \end{pmatrix} \Rightarrow h_{ij}^{TT} = 2 \frac{G}{rc^4} \ddot{Q}_{ij}$$
$$\Rightarrow h_+ = -2 \frac{G}{rc^4} 4 \omega^2 ma^2 \cos(2\omega t)$$

Source at 100 Mpc, rotating at 50 Hz, m=2  $\rm M_{sun}$  orbiting at 1000 km:  $h\!\sim\!4\!\times\!10^{-21}$ 

# Theoretical waveforms

#### Theoretical input:

- 90s: CBC PN waveforms (Blanchet, Iyer, Damour, Deruelle, Will, Wiseman, ...)
- 00s: CBC Effective One Body "EOB" (Damour, Buonanno)
- 06: BBH numerical simulation (Pretorius, Baker, Loustos, Campanelli)



# Theoretical waveforms

#### Theoretical input:

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→ Input for GW searches
→ Input for parameter estimation analyses





# LIGO Livingston, USA



Compact Binary Coalescence = CBC



Compact Binary Coalescence = CBC

L1-DCS\_CALIB\_STRAIN\_C02\_OMICRON



1186741860.8 1186741861 1186741861.3 1186741861.5 118674186<sup>1</sup>.8

167559935.8 1167559936 1167559936.3 1167559936.5 1167559936.8 30922492.6 1180922493.1 1180922493.6 1180922494.1 1180922494.6 Time [s] V1-Hrec hoft V1O2Repro2A 16384Hz OMICRON: Q=8.253 36741860.8 1186741861 1186741861.3 1186741861.5 1186741861.5 1186741860.8 1186741861 1186741861 3 1186741861.5 1186741861.8

# GW150914

# **GW151226**

# **GW170104**

**GW170608** 

# **GW170814**

8 intrinsic parameters: masses and spins

9 extrinsic parameters: distance, position (x2), orientation (x2), orbital ellipticity (x2), coalescence time and phase)



Inspiral phase: PN perturbative expansion (v/c)

Leading order  $\rightarrow$  phase evolution driven by the chirp mass (tight constraints)

- Next order  $\rightarrow$  m2/m1 and spins // L
- Next orders  $\rightarrow$  full spins



Late inspiral – merger – ringdown: numerical relativity waveforms Late inspiral  $\rightarrow$  total mass (+chirp mass + m1/m2)  $\rightarrow$  individual masses Ringdown  $\rightarrow$  final BH mass and spin



Amplitude: inversely proportional to the distance



Amplitude and phase difference between sites  $\rightarrow$  sky location + Amplitude and phase consistency





Mostly sensitive to the chirp mass  $\rightarrow m_1, m_2$  degeneracy

$$M_{c} = \frac{(m_{1}m_{2})^{3/5}}{(m_{1}+m_{2})^{1/5}}$$

GW150914	GW151226
$m_1 = 36.2^{+5.2}_{-3.2} M_{sun}$	$m_1 = 14.2^{+8.3}_{-3.7} M_{sun}$
$m_2 = 29.1^{+3.7}_{-4.4} M_{sun}$	$m_2 = 7.5^{+2.3}_{-2.3} M_{sun}$

→ All the components are black holes → Very high masses for GW150914





 $\rightarrow$  not well constrained

GW151226: at least one black hole is a Kerr black hole spin >0.2







#### GW150914

# **BBH** formation



Dynamical interactions in clusters



How can we discriminate these 2 scenarios?

 $\rightarrow$  spins!



#### Isolated binary:

Spins preferentially aligned with the binary orbital angular momentum

**Cluster binary:** Isotropic spin orientations

#### Final mass & spin



GW150914 $M_f = 62.3^{+3.7}_{-3.1} M_{sun}$  $a_f = 0.68^{+0.05}_{-0.06}$ 

GW151226 $M_f = 20.8^{+6.1}_{-1.7} M_{sun}$  $a_f = 0.74^{+0.06}_{-0.06}$ 







90% credible region for sky location:  $\rightarrow$  GW150914 = 230 deg<sup>2</sup>  $\rightarrow$  GW151226 = 850 deg<sup>2</sup>





# GW170814



	Total mass (M <sub>sun</sub> )	q=m2/m1 (M <sub>sun</sub> /M <sub>sun</sub> )	radiated energy (M <sub>sun</sub> )	effective inspiral spin	redshift	SNR
GW150914	$65.3^{+4.1}_{-3.4}$	$\frac{29.1^{+3.7}_{-4.4}}{36.2^{+5.2}_{-3.8}}$	$3.0^{+0.5}_{-0.4}$	$-0.06^{+0.14}_{-0.14}$	$0.09^{+0.03}_{-0.04}$	23.7
GW170814	$55.9^{+3.4}_{-2.7}$	$\frac{25.3^{+2.8}_{-4.2}}{30.5^{+5.7}_{-3.0}}$	$2.7^{+0.4}_{-0.3}$	$0.06^{\rm +0.12}_{\rm -0.12}$	$0.11^{+0.03}_{-0.04}$	15.0
GW170104	$50.7^{+5.9}_{-5.0}$	$\frac{19.4^{+5.3}_{-5.9}}{31.2^{+8.4}_{-6.0}}$	$2.0^{+0.6}_{-0.7}$	$-0.12^{+0.21}_{-0.30}$	$0.176^{+0.078}_{-0.074}$	13.3
GW151226	$21.8^{+5.9}_{-1.7}$	$\frac{7.5^{+2.3}_{-2.3}}{14.2^{+8.3}_{-3.7}}$	$1.0^{+0.1}_{-0.2}$	$0.21^{+0.20}_{-0.10}$	$0.09^{+0.03}_{-0.04}$	13.0
GW170608	$19^{+5}_{-1}$	$\frac{7^{+2}_{-2}}{12^{+7}_{-2}}$	$0.85^{+0.07}_{-0.17}$	$0.07^{+0.23}_{-0.09}$	$0.07^{+0.03}_{-0.03}$	13.0

#### **Testing General Relativity**

Modified dispersion relation (ex: LIV theories):  $E^2 = p^2 c^2 + A^{\alpha} c^{\alpha}$ 

massive graviton:  $\alpha = 0$ multifractal theories:  $\alpha = 2.5$ doubly special relativity:  $\alpha = 3$ extra-dimensions:  $\alpha = 4$  $\rightarrow$  modified propagation velocity:  $\frac{v_g}{c} = 1 + (\alpha - 1) \frac{AE^{\alpha - 2}}{2}$ 

	Total mass (M <sub>sun</sub> )	q=m2/m1 (M <sub>sun</sub> /M <sub>sun</sub> )	radiated energy (M <sub>sun</sub> )	effective inspiral spin	redshift	SNR
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#### **Testing General Relativity**



 $\rightarrow\,$  extra term in the evolution of the gravitational-wave phase

 $\rightarrow$  Upper limits on A

 $\alpha$ =0 A>0 : limit on the graviton mass:  $m_g < 7.7 \times 10^{-23} eV/c^2$ 





# Conclusions

- $\rightarrow$  2015: first detection of gravitational waves produced by a binary system of black holes
- $\rightarrow$  2015-2017: additional detections (5 up to now)  $\rightarrow$  initiate population studies
- $\rightarrow$  New class of stellar black holes (m > 15 M<sub>sun</sub>)
- $\rightarrow$  Parameter estimation

